MODELLING OF PERFORMANCE OF AN ARTILLERY SHELL USING NEURAL NETWORKS

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by

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CERTIFICATE



It is certified that the work contained in this thesis entitled, "Modelling of Performance of an Artillery Shell using Neural Networks" by Santosh Kumar Dehury has been carried out under our supervision and that this work has not been submitted elsewhere for a degree.

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ABSTRACT

In recent times, the most widely used trajectory modelling for artillery shells has been via mathematical models such as point mass model, modified point mass model and six-degrees-of-freedom model. Applications of these models require an a priori postulation of equations of motion governing the shell trajectory and to solve these equations, one needs reliable estimates of aerodynamic coefficients. Due to various assumptions used in arriving at the mathematical models and also due to non availability of reliable estimates of aerodynamic coefficients required to solve these equations, an alternative approach of using general function approximation capability of the feed forward neural networks (FFNNs) for estimating shell performance is explored. In the literature, no work has been reported wherein FFNNs have been used to develop neural models for shell performance. The present work addresses this aspect by way of proposing three distinct neural models for predicting trajectory variables. The models are validated for 155 mm Bofors shell HE77B data supplied in the form of range tables by ARDE, Pune. The estimated trajectory parameters like the range, the firing angle, the time of flight, etc., via the proposed neural models compare well with those listed in the supplied range tables. The neural models developed take into account variations in shell mass and its muzzle velocity, and variable atmospheric conditions like head/tail wind, crosswind, temperature and density that might prevail at the time of firing. It is shown that the proposed models can accurately predict i) the range obtainable for varying firing angles under prevailing atmospheric conditions, ii) the firing angle required to achieve desired range for known atmospheric conditions, and iii) the standard range that the shell would have achieved under standard atmospheric conditions.

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NOMENCLATURE

BAT = Ballistic Air Temperature (ambient air temperature), K

BAD, ρ = Ballistic Air Density (ambient air density), kg/m³

PW, m = Projectile mass, kg

 θ = Firing Table Elevation, Firing angle, mils

Ψ = Bearing Correction for Drift, mils

T, t = Time of flight, sec

d = Diameter of Shell, mm

W = Wind Speed, m/s

C_L, C_{Do}, C_M = Non-dimensional lift, drag and pitching moment coefficient

u = Projectile velocity, m/s

v = Projectile air-relative speed, m/s

 $\alpha_{\rm r}$ = Yaw of repose

 ω = Rotation vectors

 Ω = Earth rotation angular velocity, rad/s

g = Acceleration due to gravity, m/s^2

 I_x , I_y = Moment of inertia about x and y axis, kgm^2

P = Roll rate, spin rate of projectile, rad/s

q = Pitch rate, rad/s

R = Radius of earth, m

r = Distance from earth center to C.G. of the shell

 α = Angle of attack

h = Angular momentum

Superscripts

→ = vector quantity

= Derivative with respect to time

Subscripts

r = repose

x,y,z = component along x, y and z direction

Non-dimensional stability derivatives

$$\mathbf{C_{L_{\alpha}}} = \frac{\partial \, \mathbf{C_L}}{\partial \alpha}; \qquad \mathbf{C_{L_q}} = \frac{\partial \, \mathbf{C_L}}{\partial \left(\frac{qd}{2v}\right)}; \qquad \mathbf{C_{L_p}} = \frac{\partial \, \mathbf{C_L}}{\partial \left(\frac{pd}{2v}\right)}$$

$$\mathrm{C}_{L\dot{\alpha}} = \frac{\partial \, \mathrm{C}_L}{\partial \left(\frac{\dot{\alpha} \mathrm{d}}{2 \, \mathrm{v}}\right)}; \quad \mathrm{C}_{y_{p\alpha}} = \frac{\partial \, \mathrm{C}_y}{\partial \mathrm{p}\alpha}; \qquad \mathrm{C}_{D\alpha} 2 = \frac{\partial \, \mathrm{C}_D}{\partial \alpha^2}$$

$$\mathbf{C}_{M_{\alpha}} = \frac{\partial \mathbf{C}_{M}}{\partial \alpha}; \quad \mathbf{C}_{M_{p\alpha}} = \frac{\partial \mathbf{C}_{M}}{\partial p\alpha}; \quad \mathbf{C}_{M_{q}} = \frac{\partial \mathbf{C}_{M}}{\partial q}$$

CHAPTER 1

INTRODUCTION

Artillery forms an important wing of the army to provide firepower during war as well as during cross-boarder skirmishes with the enemy. Artillery generally falls into three basic categories: guns, howitzers and mortars. The principle difference between them being the trajectory of the round fired. A gun has a high muzzle velocity and a very flat trajectory. Normally a gun is used in a direct fire mode where the target can be seen and penetration is desirable. Howitzers have a somewhat lower muzzle velocity and arc their shells onto a target. They are used in both a direct fire and indirect fire mode. This is especially useful when an enemy is concealed behind a prepared position or the artillery men desire to have a shell explode over an enemy's head. The air-burst does less damage to hardened targets, but causes many more human casualties due to shell fragmentation covering a large area. Mortars have a very pronounced arc of flight. They have a relatively low muzzle velocity and are unsuitable for direct fire. Their principle value comes from being able to lob shells behind an obstacle, such as a fortification or a hill. They are not very accurate and dependent upon the amount of propelling powder to determine the point of impact.

The effectiveness of artillery is largely judged by the accuracy in hitting the targets. The accuracy and reliability is influenced by the design criteria used in designing the shell. Artillery shells are a class of projectiles around which much of the aeroballistic theory was originally developed, and they continue to form a significant part of the aeroballistician's interest.

Study of the motion of projectiles through an external medium is known by the name of external ballistics. If the external medium is the earth's atmosphere, then external ballistics become synonymous with aeroballistics.

Each specific projectile will have its own individual design criteria with regard to payload, range, accuracy, etc. The practical design criteria applying to a conventional artillery shell which most affect the aeroballistic aspects are:

- 1) High payload carrying potential
- Range at high charges (muzzle velocity around Mach 2-3) must be maximized hence low drag
- 3) Accuracy and repeatability
- 4) Ease of manufacturing.

The accuracy of artillery shell depends on the following major factors:

- 1) Muzzle velocity irregularity due to variation in charge
- 2) Jump and throw-off: This occurs due to recoiling effect of gun. Due to this action, there is a vertical component, known as jump, and there is a horizontal component of that force known as throw-off.
- 3) Meteorological effects like ambient temperature, density, head/tail wind, crosswind, etc.
- 4) Differences between shells due to shape, size, mass, etc.
- 5) Difference in yawing behavior, at the time of exit from the barrel, due to muzzle blast and wind consideration.

The first two factors are outside the control of the aeroballistician. The rest can be minimized by ensuring that the shell is both adequately gyroscopically and dynamically stable under all launch conditions, and has low drag.

The conventional approach hitherto for understanding the in-flight behaviour of projectiles was to develop mathematical models that could predict all elements of the trajectory from launch to target. To this purpose, it becomes essential that all forces, moments and other terms (e.g., coriolis force due to the rotation of the earth) affecting the flight of the projectile are accounted for in a well defined mathematical form¹. Beginning with the most simple but relatively inaccurate mathematical model, the in-vacuo trajectory model, more and more sophisticated models of increasing accuracy such as the point mass model, the modified point mass model and the six-degrees-of-freedom model have been developed. A brief description of these models is given in chapter 3. Presently, we only wish to point out that even the best of these proposed models have their limitations due to their inability to model all the problem variables adequately. For example, the initial conditions at the time of shell leaving the barrel are not accounted for by any of the proposed mathematical models. Furthermore, the models require aerodynamic coefficients as input (e.g., drag coefficient, damping in roll derivative C_{lp} lift curve slope C_{La}, etc.) and the estimates available for these coefficients are not so reliable. Finally, the varying atmospheric conditions over the height traversed by the projectile are accounted for only in an adhoc manner by using one single weighted mean value of the variables like temperature, density, head/tail wind and crosswind.

It is thus realized that even the best of the mathematical models available to date are not reliable for field application because accurate predictions are difficult for: 1) the range obtainable for various firing angles, 2) the firing angle required for specified range.

The limitations of the mathematical models so far used for predicting the performance of artillery shell motivated us to look at an alternative approach to modelling. The feed forward neural network^{2,3,4} provides one such potential way of modelling.

The neural networks have been successfully used in such diverse fields as signal processing, pattern recognition, system identification and control. In recent years, neural models of aircraft aerodynamics have been successfully developed for many applications relevant to Aerospace Engineering^{5,6,7}. For example, neural modelling has been used for estimating aircraft stability and control derivatives of stable^{8,9,10}, unstable¹¹, aeroelastic aircraft¹². It was envisaged that a neural model can be developed to replace the use of hitherto used mathematical models for solving the shell trajectory related problems.

For real life situations, it was realized that the problem of shell trajectory, broadly speaking, could be divided into three categories: Under prevailing ambient atmospheric conditions 1) to predict range for the chosen firing angle, θ , 2) to predict required firing angle to achieve specified range, 3) to predict range that would have been achievable under standard atmospheric conditions, using the range data obtained under existing atmospheric conditions. The next step is to identify the relevant set of input-output variables for the network for each of these problems. Finally, a suitable architecture for the Neural Networks is to be searched to achieve acceptable functional mapping between the input-output variables for each of the problem.

In the present work, all the above problems are addressed and adequately solved. For demonstrating the prediction capability of neural models developed, the data used is for the 155mm Bofor shell, supplied by ARDE, Pune. Details of the data supplied and its use for testing various neural models is given in chapter 3. The details of modelling for the three categories of problems related to the shell trajectory, along with results obtained from each of three models are discussed in chapter 4. A brief overview of the neural network precedes these chapters 3 and 4, and is given in chapter 2. The dissertation ends with chapter 5 containing conclusions and a few suggestions for the future work.

CHAPTER 2

ARTIFICIAL NEURAL NETWORK

2.1 Introduction

A neural network is a parallel distributed processor that has a natural propensity for storing experimental knowledge and making it available for use. It resembles the brain in two respects, 1) Knowledge is acquired by the network through learning process, 2) Inter neuron connection strengths known as synaptic weights are used to store the knowledge. Neural networks are also referred to in the literature^{2,3,4} as neuro computers, connectionist networks, parallel distributed processors, etc.

Artificial neural networks consist of group of neurons arranged in a layered structure. Each neuron receives signal from the neurons in the layer previous to itself and passes a signal on to the neuron in the following layer. The relationship between the summed inputs to a neuron and its output is governed by an 'activation function'. Some of the commonly employed activation functions are the step functions, the tangent-hyperbolic function, and the logistic (sigmoidal) function.

Out of these, the most often-used activation function is the sigmoidal function defined as

$$F(x) = \frac{1}{1 + e^{-x/\lambda}}$$

where λ is the logistic gain.

The sigmoidal function is continuous, monotonically increasing and continuously differentiable, and it asymptotically approaches fixed finite values as the input approaches infinity (+ or -).

Amongst the artificial neural networks, the feed forward neural networks (FFNNs) have found the favour with most researchers for applications in aerospace engineering problems^{5,6,7}. The feed forward neural network consists of source nodes that constitute the input layer and one or more hidden layers and an output layer. Feed forward neural networks have neurons arranged in layers like directed graphs, implying a unidirectional flow of signals, and thus are static in nature. This kind of modeling develops input-output relationship of a black-box kind. Each of the connection between neurons is assigned its individual weight and it is adjusted so as to yield the required output corresponding to the known set of inputs. Assignment of weights is done during the training sessions of the network.

2.2 Back Propagation Algorithm

One of the efficient methods for training the FFNN is the back propagation algorithm (BPA). Back propagation algorithm consists of a forward and backward pass through different layers of the network. During the forward pass, the input vector is applied to the input nodes of the network and its effect propagates through the network layer by layer. The connective weights are all kept fixed during the forward pass. On the other hand, in the backward pass, the weights are updated in accordance with error correction rule. Specifically, the actual response of the network is subtracted from the desired response to produce

an error signal. This error signal is then propagated backward against the direction of the connective weights. There are the four steps for back propagation algorithm.

- a) Initialization: Start with a reasonable network configuration and set all the synaptic weights randomly.
- b) Forward Computation: Let a training example represented by x(n) be applied to the input nodes. Then the output of the network is computed by proceeding through the network, layer by layer. Next, the error signal is computed using difference between the desired response vector and the output vector.
- c) Backward Computation: The back propagation algorithm is based on optimizing a suitably defined error function. At each point, the local output error cost function defined by the sum of the squared error is computed. The weights of the network are adjusted in such a way that the mean squared error (MSE) is minimized.

The MSE is given by

$$MSE = \frac{1}{m \times n} \sum_{i=1}^{m} \sum_{j=1}^{n} [Yi(j) - Xi(j)]^{2}$$

where Y and X are the desired and predicted outputs, n is the number of data points and m is the number of output variables.

d) Step (b) to (c) are repeated for each training pair in the training set until the error for the entire set is less than the prescribed value or the number of iterations exceed the prescribed limit.

The training algorithm is recursive in nature and it needs repetitive training sessions to achieve the required learning. There are many network influential (tuning) parameters like the learning rate, the momentum rate, the number of hidden layers, the number of iterations, the logistic gain, etc., that affect the accuracy of functional mapping between the input and the output variables. There are no set rules for fixing values of these influential parameters. In literature, a few guidelines are available to guide the choice of these parameters. However, the final choices of fine tuning these parameters is to be achieved by trial and error for the given problem, and it is a crucial step in finding a suitable neural model for the problem. Some of the guidelines and thumb rules for training of neural network are given in Appendix B.

The neural network model is first trained on the known sets of inputoutput pairs of experimental or recorded data. The trained network is then capable
of predicting the required output based on known (measured) input variables. This
approach does not require a mathematical model or a transfer function relating the
input-output data but only a sufficient set of input-output pairs of data. The choice
of inputs that are likely to affect the output to be predicted by the neural model is
of critical importance. The selection of inputs for the given problem is based on
the understanding of the physics of the problem and engineering judgement.

In the present work, a neural model is proposed for the trajectory modelling of an artillery shell fired from a gun. A non-linear relationship is mapped by the neural network between the input variables such as range, muzzle velocity, wind velocity, ballistic air temperature (BAT), ballistic air density

(BAD) with the output variables such as time of flight (T), bearing corrections for drift (Ψ) and angle of firing (θ). A schematic of such a neural model is shown in fig.1. For a typical neural model used in the present work, Fig.1, the choice of the input and output variables for mapping projectile dynamics is dictated by the physical understanding of the phenomenon governing the shell dynamics. Once the input and output variables for the feed forward artificial network (FFNN) are selected, the FFNN model of shell dynamics is achieved without the need of a formal model structure formulation.

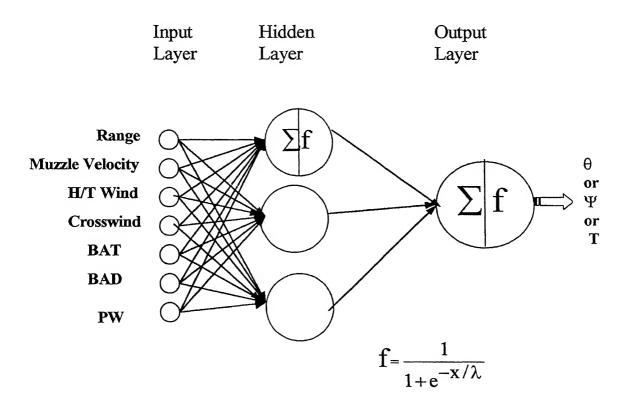


Fig. 1 Schematic of feed forward neural network.

CHAPTER 3

TRAJECTORY AND RANGE MODELLING OF ARTILLERY SHELL

3.1 General

Artillery shells are a class of projectiles around which much of the aeroballistic theory was originally developed. Even today, it still continues to be of interest and further investigations for many aeroballisticians and user agencies. In the present work, we are specifically to focus on flight of a spin stabilized, dynamically stable, conventional artillery projectile, possessing either rotational or some form of mirror symmetry. For such projectiles, there are two major factors that differentiate their aerodynamics from the classical aerodynamics of, say, aircraft aerodynamics:

- 1) The geometric symmetry of the projectile implies that many aerodynamic terms are themselves symmetric. For example, for a shell with cruciform tails will have aerodynamic derivatives $Cm_{\alpha} = -Cn_{\beta}$ and $Cm_{q} = Cn_{r}$.
- 2) The second factor to be considered is due to spin rate imparted to many shells, giving rise to aerodynamic effects that are unique to aeroballistics. For example, the magnus forces and moments are hardly of concern for aircraft dynamics, but may play significant role for shell dynamics.

Presently, the conventional approach to modelling of trajectory and range of artillery shell has been by postulating a suitable mathematical model consisting of equations of motion. There are numerous such forms of trajectory model involving different basic assumptions and having different complexities of solution. We shall briefly outline, in an increasing order of complexities and accuracy, the more commonly utilized analytical trajectory models used at present time.

3.2 The in-vacuo trajectory model

In the in-vacuo trajectory model all aerodynamic forces and moments acting on the projectile are neglected. It is thus highly inaccurate for all but the shortest-range trajectories and the lowest drag projectiles. However, it does have its uses, in defining concepts such as trajectory rigidity, and also for setting limits on parameters such as range and vertex height. The simplicity of the model renders analytical solution easily.

3.3 The point mass model

In this model, it is assumed that the only aerodynamic force acting on the projectile is drag. It provides fairly accurate estimates of range for adequately stable projectiles and can also be used to estimate the first order effects of wind. The point mass model is given as below.

$$\frac{\mathrm{d}^2 x}{\mathrm{d}t^2} = -\frac{\pi \rho \mathrm{d}^2 C_D}{8\mathrm{m}} \, \mathrm{v} \left(\frac{\mathrm{d}x}{\mathrm{d}t} - \mathrm{W}_{\mathrm{X}} \right) \tag{1a}$$

$$\frac{d^2y}{dt^2} = -g - \frac{\pi \rho d^2C_D}{8m} v \left(\frac{dy}{dt} - W_y\right)$$
 (1b)

$$\frac{d^2z}{dt^2} = -\frac{\pi \rho d^2C_D}{8m} v \left(\frac{dz}{dt} - W_z\right)$$
 (1c)

where x denotes range, y denotes height, z denotes drift and W_x , W_y , W_z are, respectively, the x, y and z components of the wind velocity W. This model, however, does not account for the effect of spin of the shell and thus fails to predict the drift due to magnus moment. Also, it neglects the lift forces acting on the shell.

3.4 The Modified point mass model

The modified point mass model is also known as 4 degree-of-freedom model (3 spatial degrees-of-freedom plus axial spin). Its basis is a conventional point mass, in addition, the instantaneous equilibrium yaw is calculated at each time step along the trajectory so as to provide estimates of yaw, drag, drift and magnus force effects resulting from the yaw of repose. The modified point mass equations of motion are given as

$$\frac{d\vec{u}}{dt} = -\frac{\pi \rho d^2}{8m} \left(C_{D_O} + C_{D_Q} 2 \alpha_r^2 \right) v \vec{v} + \frac{\pi \rho d^2}{8m} C_{L_Q} v^2 \alpha_r - \frac{\pi \rho d^3}{16m} C_{y_{pq}} p(\alpha_r \times \vec{v}) - g_O \frac{R^2}{r^3} \vec{r} + 2(\omega \times \vec{u})$$
(2a)

$$\frac{\mathrm{dp}}{\mathrm{dt}} = \frac{\pi \rho \mathrm{d}^4}{16\mathrm{I}_{\mathrm{X}}} \mathrm{pvC}_{\mathrm{lp}} \tag{2b}$$

$$\alpha_{r} = -\frac{8pI_{x}}{\pi \rho d^{3}C_{M_{C}}} \frac{\left[\vec{v} \times (d\vec{u}/dt)\right]}{v^{4}\alpha_{r}}$$
(2c)

The quantities in the above equation are defined as follows:

$$\vec{u} = \frac{d\vec{x}}{dt}$$
, $\vec{v} = \vec{u} - \vec{W}$, $\vec{r} = \vec{x} - \vec{R}$, $\vec{R} = (0, -R, 0)$ [\vec{W} denotes the wind vector]

 $\vec{\omega} = (-\Omega \cos[\text{latitude}]\cos[\text{azimuth}]$

 Ω sin[latitude],

 Ω cos[latitude] sin[azimuth])

where $\Omega = 7.29 \times 10^{-5}$ rad/s (rotation of the earth),

R = 6370320 m (radius of the earth),

 $g_o = 9.80665[1-0.0026373 \cos(2\times \text{latitude}) +0.0000059 [\cos(2\times \text{latitude})]^2].$

The axis system used is as for the point mass model with \vec{x} being along the line of fire.

As may be seen from the above equations, the aerodynamic coefficient input required is extensive and accuracy of these aerodynamic coefficients is crucial for reliable estimates of range. However, for most artillery shells, the reliability of estimated values of aerodynamic coefficients is not high enough to inspire confidence in resulting range estimates from this model. In spite of this limitation, this model has the capability of providing reasonable accounts of end point data. It can estimate wind corrections and can accept non-linear aerodynamic inputs if required. However, because the equation for calculating yaw of repose assumes quasi-linear aerodynamics, the use of non-linear aerodynamics in equations is questionable.

3.5 The six-degree-of-freedom model

As a final step, the most sophisticated trajectory model developed was the sixdegree-of-freedom model having the 3 spatial degrees of freedom, yaw degree of freedom in two planes and the spin. In this model there are no assumptions concerning linearised aerodynamics or projectile symmetry. However, the indeterminability of many of the initial conditions and aerodynamic coefficients which are required as input frequently results in the model not giving significantly better end results than the modified point mass model. Thus its usage might not be justified for routine fire control work. It is nevertheless a powerful tool for the ammunition designer.

The six-degree-of-freedom model equations are given as

$$\begin{split} \frac{d\vec{u}}{dt} &= -\frac{\pi \rho d^2}{8m} \left(C_{D_0} + C_{D\alpha}^2 \alpha^2 \right) \vec{v} \vec{v} \\ &+ \frac{\pi \rho d^2}{8m} C_{L_{\alpha}} \left[\vec{v} \times (\vec{x} \times \vec{v}) \right] \end{split} \tag{Drag}$$

$$+\frac{\pi \rho d^2}{8m} C_{L\alpha} \left[\vec{v} \times (\vec{x} \times \vec{v}) \right]$$
 (Lift)

$$\begin{split} &+\frac{\pi\rho d^3}{16m}C_{yp\alpha}\frac{I_y}{I_x}\big(\bar{h}\cdot\bar{x}\big)(\bar{x}\times\bar{v}\big) \qquad \qquad \text{(Magnus Forces)} \\ &+\frac{\pi\rho d^3}{16m}\Big(C_{L_q}+C_{L_{\dot{\alpha}}}\Big)v\big(\bar{h}\times\bar{x}\big) \qquad \qquad \text{(Damping Forces)} \\ &-g_0\frac{R^2}{r^3}\bar{r}+2\big(\bar{\omega}\times\bar{u}\big) \qquad \qquad \text{(Gravity and Coriolis)} \qquad \qquad \text{(3a)} \\ &\frac{d\bar{h}}{dt}=\frac{\pi\rho d^4}{16I_x}C_{I_p}\big(\bar{h}\cdot\bar{x}\big)v\bar{x} \qquad \qquad \text{(Spin Damping)} \\ &+\frac{\pi\rho d^3}{8I_y}C_{M\alpha}v\big(\bar{v}\times\bar{x}\big) \qquad \qquad \text{(Overturning Moment)} \\ &-\frac{\pi\rho d^4}{16I_x}C_{M_{p\alpha}}\big(\bar{h}\cdot\bar{x}\big)\big[\bar{x}\times\big(\bar{x}\times\bar{v}\big)\big] \qquad \qquad \text{(Magnus Moment)} \\ &+\frac{\pi\rho d^4}{16I_y}\Big(C_{M_q}+C_{M_{\dot{\alpha}}}\big)v\big[\bar{x}\times\big(\bar{h}\times\bar{x}\big)\big] \qquad \qquad \text{(Damping Moment)} \\ &\text{where} \\ &\alpha=\cos^{-1}\big[\big(\bar{v}\cdot\bar{x}\big)/v\big] \\ &\text{and } I_y\bar{h} \text{ is the angular momentum vector.} \end{split}$$

3.6 Range Tables for B-Shell

As mentioned earlier, due to non availability of real firing data, the range tables for the 155mm Bofors shell HE 77B (here after referred to as B-shell for convenience) are used for the present study. These tables and the explanatory notes (given in Appendix A) were supplied by ARDE, Pune. The range table lists range obtainable for various firing table elevations (hereafter referred to as firing angle, θ) under standard calm atmospheric conditions and for nominal values of weight and muzzle velocity. Also time of flight and correction to bearing drift is provided. The corrections to these listed values of range for each value of θ due to following variations at the time of firing are also provided:

1) Variations in ambient atmospheric conditions (temperature, density)

- 2) Head/tail wind
- 3) Crosswind
- 4) Change in weight and muzzle velocity from the corresponding nominal value.

The range tables have been prepared using the modified point mass trajectory model. As pointed out earlier, this model suffers from a few limitations, mainly because of the not-so-reliable accuracy of aerodynamic coefficients that need to be used to solve the equations of motion. The complete six-degree-of-freedom model would also suffer for the same reasons. Even if accurate aerodynamic coefficients were available, there are few other uncertainties that would affect the range estimates in real life and cause dispersion of shells. A few such uncertainties are briefly outlined below:

1. Slight differences between nominally similar projectiles

Any differences in mass, shape, surface finish, etc., will cause changes in the trajectory of the projectile to some extent. Projectiles might suffer from two types of asymmetries while passing through the manufacturing stage: Configurational asymmetries and inertial asymmetries. The inertial asymmetries may be of mass unbalances wherein center of mass is not on the geometrical axis of symmetry and dynamic unbalance where the principal axis of inertia is not collinear with this axis. These asymmetries can lead to large dispersions, and it is by keeping manufacturing tolerances to minimum, and by imparting some amount of spin that one can reduce the dispersion due to this effect. However, spin rate is to be carefully chosen to avoid the spin-yaw resonance zone.

2. Meteorological conditions

It is noted that the solution of equations of motion uses a single value for head or tail wind and crosswind. Furthermore, the corrections to the range (tabulated for standard atmospheric conditions) for variation in temperature and density are incorporated by using a single value of temperatures and density at the location of firing. It is realized that the shell will be passing through different wind and atmospheric conditions of temperature and density as its altitude varies during its inflight trajectory. However, for the purpose of applying corrections, a weighted mean value of wind velocity, temperature and density is used to account for varying conditions prevailing at different altitudes.

3. Variable launch conditions: Variation in muzzle velocity, gun-jump and throwoff, initial yaw, etc.

At the time of shell leaving the gun barrel, the initial conditions experienced by the shell are not identical for all the shells. In particular, the initial velocity of shell (muzzle velocity) depends upon the charge concentration at the time of firing.

For the spun projectiles crosswind has an effect in the vertical plane due to the time taken to adapt to the air-relative zero yaw position. This occurs whenever the projectile emerges into a region of significantly different wind-relative zero yaw attitude, but most commonly has its effect on a projectile exiting from the launcher. Unlike the downward carry effect, which is usually roughly quadratic in range and depends on the wind at all points down-range, this effect is called aerodynamic jump, which is linear in range and dependent on wind at one point. There is a similar term due to the transverse component of a head wind. The total effect is called windage jump.

The initial yaw and yawing rate of a projectile will obviously determine to a large extent what yaw levels are present in the early stage of the trajectory. Furthermore, if the damping is poor, they may lead to consistently high yaw and thus cause dispersion in range due to yaw drag, especially with indirect fire munitions.

3.7 The Neural Models

The limitations of the mathematical models so far used for predicting range of artillery shells motivated us to look at an alternative approach to modelling. The feed forward neural network provides one such potential way of modelling. The neural model needs identification of suitable input-output variables to map the relationship existing between them. The functional relation is obtained by training with measured input-output variables and then the trained network is used to predict the output for set of inputs not seen by network during the training phase. The data from the range table provided by ARDE, Pune for B-shell is used for the present work.

For the purpose of developing a neural model, the data from the range table was randomly selected to form sets having chosen number of data points, say, 100 or 50 or 25 or 15. One of these sets is used for training the network. Then two sets of data points, each of 30 are taken for validation sets, which are different from the training set. These two sets are used to verify the acceptability of the trained network. As mentioned in Appendix B, the acceptability of the network architecture is decided by comparing the MSE during training phase and validation phase. The thumb rule applied is that MSE for the two validation sets should be not greater than about two times the MSE for the training set. Of course, the MSE permitted on the training set is prescribed and kept below it, while choosing the architecture of the network, i.e., while choosing the learning

rate, the momentum rate, the number of iteration, the number of neuron, etc. Finally, one set of data, not used for the above two stages of training or validation is used to predict the required output. This output is compared with the known output corresponding to the same inputs, and thus shows acceptability of the neural model in predicting the required output variables.

From application point of view, the following three types of modelling problems were taken up for study. The neural network modelling for these three cases are presented in details in the next chapter along with the results obtained via each of these models. However, a brief outline of the three models is given below.

Model 1

This model deals with the direct problem of modelling Range, time of flight, and drift experienced by the B-Shell. These output variables of the neural model would depend on the firing angle θ , air temperature and density, head/tail wind, crosswind, muzzle velocity, weight of shell and the initial conditions.

Model 2

This model deals with the inverse problem of predicting the firing angle θ required to achieve desired range, given the air temperature and density, head/tail wind, crosswind, muzzle velocity, weight of the shell. It also predicts time of flight and drift. This is what a user (soldier) would require to know in most of the real life applications.

Model 3

This model was developed to predict the range that would be obtainable under standard conditions, given the measured data of range obtained under varying atmospheric conditions like temperature, density, head/tail wind, crosswind, muzzle velocity, and shell weight. Such a prediction capability would be useful to compare performance of different shells under identical (standard) conditions. It is not practical to obtain data for different shell or for the same shell on different days under similar conditions, and thus compare the relative performance. If data collected under different ambient conditions can be used for training the network, and then be able to predict the range that would result under chosen standard ambient conditions, one could then compare results for the different shells or the same shell fired at different times or days.

As a subset of this model, attempt was also made to estimate sensitivity coefficients (partial derivatives) that would show how the range is affected by variations in each of input variables. These sensitivity coefficients were in turn used to obtain standard range from the range data corresponding to ambient conditions of temperature, density, wind, etc.

The results and discussions for all the above three models, along with details of modelling are presented in the next chapter.

CHAPTER 4

NEURAL MODELS, RESULTS AND DISCUSSION

In this chapter, we first analyse the data of B-shell supplied by ARDE, Pune. Next, details of all the three models mentioned in the previous chapter are presented. Finally, the results for all the neural models are discussed.

4.1 Analysis of B-shell data

The data sets, explanatory notes and geometric, mass and moment of inertia characteristics of B-shell supplied by ARDE, Pune are given in Appendix A. The data tables (Table F (i) and Table F (ii)) contain range data for firing table elevation (Firing angle) from 0 mil to 1298.4 mils. These firing angles correspond to variation from 0° to 70° (360° = 6400 mils). Table F (i) has the basic data for range (X, col 1) along with the time of flight (t, col 7), correction to bearing for drift due to spin ($\Delta_{C}A_{d}$, col 8) and correction to bearing for 1 knot crosswind ($\Delta_{\rm C}A_{\rm B}$ col 9) obtainable for varying firing angles (A_E, col 2) at sea level under standard atmospheric conditions. Tables F (ii) gives corrections to range for the non-standard conditions. Corrections to be applied to calculate the range at various firing angles for variation from the nominal values of muzzle velocity, projectile weight, air temperature and density, and for mean weighted head/tail wind are tabulated. In Table F (ii), column 2 gives correction for muzzle velocity being 1m/s higher or lower than nominal value, column 3 gives correction for 1knot head/tail wind, column 4 and 5 give, respectively, corrections for 1% higher or lower value of temperature and density as compared to those for standard atmosphere, column 6 gives correction for weight of shell being 1 unit (1 unit = 0.45 kg) higher or lower than its nominal value. The nominal values of the B-shell and its geometry are given in fig. A1 of Appendix A. Explanatory notes on the terminology used in Range table is given following the range table in Appendix A.

The range table F (i) and F (ii) were used to prepare input-output data sets for the neural models. The range R for non-standard conditions was calculated as follows:

$$R = X + C_1(\Delta V) + C_2(W_x) + C_3(\% BAT) + C_4(\% BAD) + C_5(\Delta PW)$$
(4.1)

where X = Range at standard condition for a particular firing table elevation (firing angle, θ).

 C_1 = Correction to range for muzzle velocity being higher or lower by 1m/s than the nominal velocity, given in column 2 of the table F(ii) of appendix A., sign of C_1 is negative if velocity lower and positive if velocity is higher than the nominal value.

 ΔV = Muzzle velocity - nominal value of 818 m/s.

C₂ = Correction to range for 1 knot head/tail wind, shown in column 3 of table
F(ii) of Appendix A, sign is negative for head wind and positive for tail wind.

 W_x = Weighted mean value of head/tail wind.

C₃= Correction to range for temperature being 1% higher or lower than value in standard atmosphere, given in column 4 of table F(ii) of appendix A, sign is negative for temperature being higher and positive for it being lower than standard value.

% BAT = (Actual BAT - BAT in Standard atmosphere) \times 100/Actual BAT C_4 = Correction to range for density being 1% higher or lower than value in

standard atmosphere, given in column 5 of table F(ii), sign is negative for density being higher and positive for it being lower than standard value.

% BAD = (Actual BAD - BAD in Standard atmosphere) \times 100/Actual BAD

C₅ = Correction to range for 1 unit change in projectile weight, given in the column 6 of the table F(ii) of Appendix A, sign is negative for weight being higher and positive for being lower than the nominal value of 42.6 kg

 $\Delta PW = (Actual weight of Shell - 42.6)$

It is noted that the crosswind gives rise to drift in the lateral direction but does not affect the range.

To illustrate the calculation of range R for non-standard conditions, the following example is presented:

Consider the range for firing angle of 67.2 mils. The Table F(i) gives the standard range X=6600 m, the time of flight = 10.2 sec, correction to bearing for drift $\Delta_{\rm C}A_{\rm d}=2.8$ mils and correction to bearing for 1 knot crosswind $\Delta_{\rm C}A_{\rm B}=0.17$ mils.

Let us assume that the muzzle velocity is 819.9 m/s, tail wind is 8.01 knots, crosswind is 8.7 knots, projectile weight is 43.1769 kg, air temperature and density are 297.381K and 1.2676 kg/m³ respectively. For the firing angle of 67.2 mils, from table F(i) and F(ii), we have

 $C_1 = -13.0 \text{ m} / \text{m/s}$

 $C_2 = -1.7 \text{ m/knot}$

 $C_3 = 4.4 \text{ m} / 1\%$ change in BAT

 $C_4 = 17.9 \text{ m} / 1\% \text{ change in BAD}$

 $C_5 = 13 \text{ m} / 1 \text{unit change in projectile weight}$

For the chosen values, the following quantities are easily calculated

 Δ Muzzle velocity = Δ V = 1.9 m/s,

 Δ Projectile weight = Δ PW = 1.282 unit,

% change in BAT = 3.2,

% change in BAD = 3.479,

Substituting above value in Eq. (4.1), we get the non-standard range:

$$R=6600 - [(-13.0 \times 1.9) + (-1.7 \times 8.01) + (4.4 \times 3.2) + (17.9 \times 3.479) + (13 \times 1.282)]$$

$$= 6545.3 \text{ m}.$$

Bearing Correction (Ψ) = Correction to bearing for drift + Correction to bearing for crosswind.

$$\Psi = 2.8 + (8.7 \times 0.17) = 4.279$$
 mils

The implication of the bearing correction is that the projectile would drift to the right (looking from behind in the direction of firing) by angle Ψ . To hit the target, the shell is fired by aiming to the left by angle Ψ and this would, in turn, ensure that the target is hit after the drift that the shell will experience due to spin and crosswinds.

Following the above procedure, the data given in the range tables for B-shell was converted into a convenient form for its use in neural models to be developed. Specifically, the data yielded sets of data, each set having standard range X, non-standard range R, time of flight T, drift angle Ψ , ambient temperature and density, crosswind, head or tail wind, variation from the nominal value of muzzle velocity and projectile weight, or percent variation thereof.

4.2 Modelling

The data sets generated from the range tables of B-shell were used for training the neural models. However, random selection of input-output pairs for any of the models (briefly described in chapter 3) showed poor training. A close look at the data and considering the physics of the projectile motion gave the clue: as is well known for idealized point mass projectile motion in vacuum, the range increases as the angle of projections increases from 0 to 45 degrees and then decreases as angle increases from 45 to 90 degrees, the maximum range being at 45 degrees. A similar trend was observable for the B-shell and maximum range was just above 45 degrees (802 mils). The implication of this fact is that same range is attained for two distinct values of angle of firing, one below 45 degree and other above 45 degree. Thus the neural network sees inherent contradiction in data and hence the difficulty in mapping the data spanned across all the values of firing angles.

To resolve the above difficulty, the data was partitioned into two bins: one having data for firing angle from 0 to 45 degree and the other from 45° to 70° (firing tables gives data up to 70° only). The neural models for these two were separately developed. It may be pointed out that, such an approach will not create any difficulty in real-life applications because the requirements about the desirable firing angle to be less than or more than 45 degree would be known - if the shell is to achieve higher altitude during its flight to target, the firing angle of greater than 45 degree would be recommended, otherwise less than 45 degree would be the preferred option due to shorter time of flight.

For the purpose of modelling, a set of randomly selected input-output data was selected from each bin. Sets of varying number of input-output samples were tried to arrive at the minimum number of samples required for adequate training level. It is realized that in real life, the number of samples available will be limited due to the cost involved in collecting such range data, and hence the need to search for the minimum number of data samples to get an acceptable neural model. The numbers of samples tried were 100, 50, 25 and 15. Higher number of samples obviously led to better training, but even as few as 15 samples also gave satisfactory models. The suitability of the model is tested by a test (validation) set of data, typically consisting of 30 input-output samples, selected randomly from the range table; if the MSE was only of the order of two times the MSE prescribed for the training phase, the neural model was accepted and its architecture fixed for the prediction phase. If not, the architecture was varied till it met the above conditions on MSE for training and validation phase.

Once the neural model is validated, it is used for the prediction purpose. For prediction, a set of randomly selected data is taken from the range table, and only the input variables of this set are treated as known while the output variable is predicted by the neural model. Since the output is also known from the range table, it is compared with the neural model output to show how well the predicted values compare with the known values. Typically, for prediction, 10 samples were randomly selected from the range table.

In case of neural models like Model 1 and Model 2, prediction of more than one output was required, e.g., Model 1 is to predict range, bearing correction and time of flight. In view of this, the neural models having more than one output were subjected to

the following test: for the same set of inputs, is it better to train the network separately for one output at a time, or train it on all the outputs at once. It was observed that even though the latter option gave reasonable predictions of all outputs, the former option always yielded relatively more accurate predictions. The accuracy being of prime concern, it is worthwhile to have separate neural models for each of the output variables and, therefore, all studies repeated herein are based on the single output predictions.

Because the above details of the procedure are common to all the models discussed next, we shall refrain from repeating it and only point out wherever the procedure differs in some significant way from the above mentioned guidelines. Results for the various models discussed next are presented in tabular as well as in graphical form.

4.3 Model 1

In model 1, we wish to develop neural model for predicting range(R), bearing correction (Ψ) and time of flight (T). These would, therefore, form the output variables of the neural model. These output variables depend on the firing angle (θ), ballistic air temperature (BAT), ballistic air density (BAD), muzzle velocity (V), projectile weight (PW), head/tail wind (W_x) and crosswind (W_z). Thus the neural model has R, or Ψ , or T as the output variable and θ , BAT, BAD, V, PW, W_x , W_z as the input variables. The input variables V, BAT and BAD are given in percent variation from the nominal values – nominal muzzle velocity being 818 m/s, and nominal BAT and BAD being sea level values in standard atmosphere. The Δ PW value was given as the difference between the actual projectile mass and the nominal projectile mass (42.6kg). The schematic of such a model is shown in fig. 2.

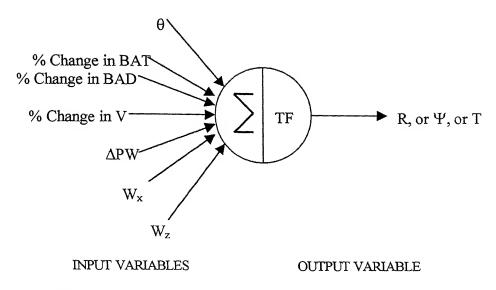


Fig. 2 Schematic Representation of FFNN For model 1

As mentioned earlier, input-output samples were randomly selected from the range table for B-shell. Although training was carried out for data sets having 100, 50, 25 and 15 samples, the results for the most stringent case of data set having 15 samples are presented. For data set having higher number of samples (> 15), the training was always superior to that for 15 samples. For illustration, MSE for 15 samples and 100 samples as a function of iteration is shown in fig.3. It is noted that the minimum MSE is achieved faster in case of 100 samples (in less than 200 iterations) as compared to 15 samples (in about 300 iterations). Furthermore, the value of minimum MSE achieved in case of 100 samples is about 8.22×10⁻⁸ where as for the case of 15 samples, it is 7.64×10⁻⁶, which is two orders of magnitude higher than for 100 samples. Fig. 3 also shows MSE for the two test data (30 samples) for both cases. It is seen that the MSE for both test data is of the order of two times the corresponding MSE values for 15 and 100 samples.

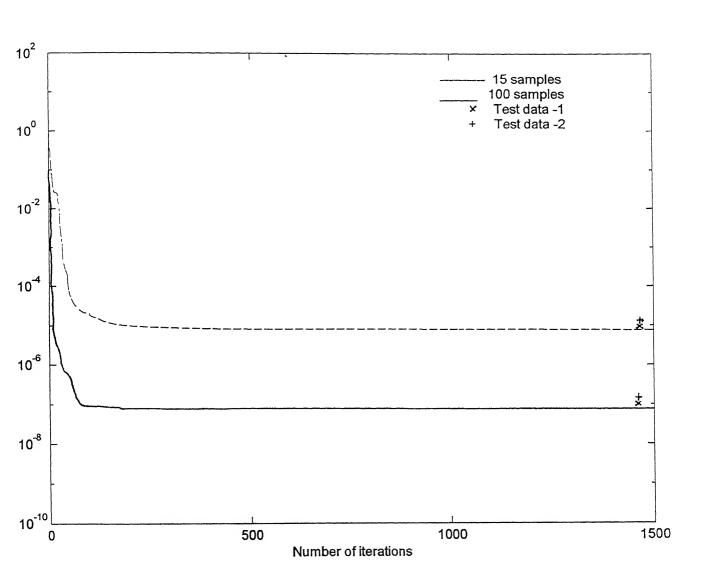


Fig. 3 Comparison of MSE for 15 and 100 training samples

Notwithstanding the superior training for the case of 100 samples, for the case of 15 samples, in absolute terms, the training level achieved was satisfactory, as also was the validation test. Hence, all the results presented are only for the case of 15 samples.

For randomly selected 15 samples of θ , BAT, BAD, V, PW, HT and W_z , the corresponding R, Ψ and T were calculated as explained in 4.1. In addition, two other sets of 30 samples each were similarly generated for use as test data. The network tuning parameters were varied till acceptable network training was achieved as per criteria set out in Appendix B. Now a set of 10 samples, randomly taken from the range table, is used to predict R, Ψ and T. The results are given in Table 1 and graphically compared with the actual values in Fig. 4. As may be seen, the predicted values compare well with the actual values.

4.4 Model 2

This model is the one, which would be of more use in real-life applications. A soldier would want to know the firing angle (θ) he should use, the bearing correction (Ψ) he should apply and the time of flight (T) for shell to reach the target. The time of flight is required to set the fuse such that the shell explodes after a fixed time – the time being chosen to be just prior to shell reaching the target and thereby ensuring that shell explodes in air, just before hitting the ground. The information made available prior to firing of the shell is the ambient atmospheric conditions: head/tail wind (W_x), crosswind (W_z), muzzle velocity (V), projectile weight (PW), atmospheric temperature (BAT) and density (BAD). Thus, for the desired range under the prevailing atmospheric conditions, we wish to develop a model that would predict the firing angle, bearing correction and time of flight. The schematic of such a model is shown in fig. 5.

Table 1. Model 1: Comparison of Actual and Predicted Range, Bearing correction (Ψ), Time of flight (T) for the given value of θ

θ in	Ran	ge in m	Ψin	Mils	Ti	n sec
Mils	Actual	Predicted	Actual	Predicted	Actual	Predicted
7.7	1000.8	1000	0.097	0.098	1.301	1.3
11.8	1498	1498.5	0.579	0.573	1.898	1.89
25.3	3019.3	3020	-0.071	-0.07	4.119	4.12
35.5	3981.6	3983	2.073	2.075	5.563	5.561
40.9	4447.8	4446	3.557	3.56	6.348	6.34
52.7	5424.6	5423	3.604	3.6	8.049	8.05
65.8	6406.9	6406	5.545	5.5	9.814	9.82
72.9	7053.1	7051	1.843	1.845	11.106	11.1
88.4	8045.9	8046.5	5.227	5.22	13.296	13.3
96.9	8195.3	8194.6	8.991	9	13.6	13.61

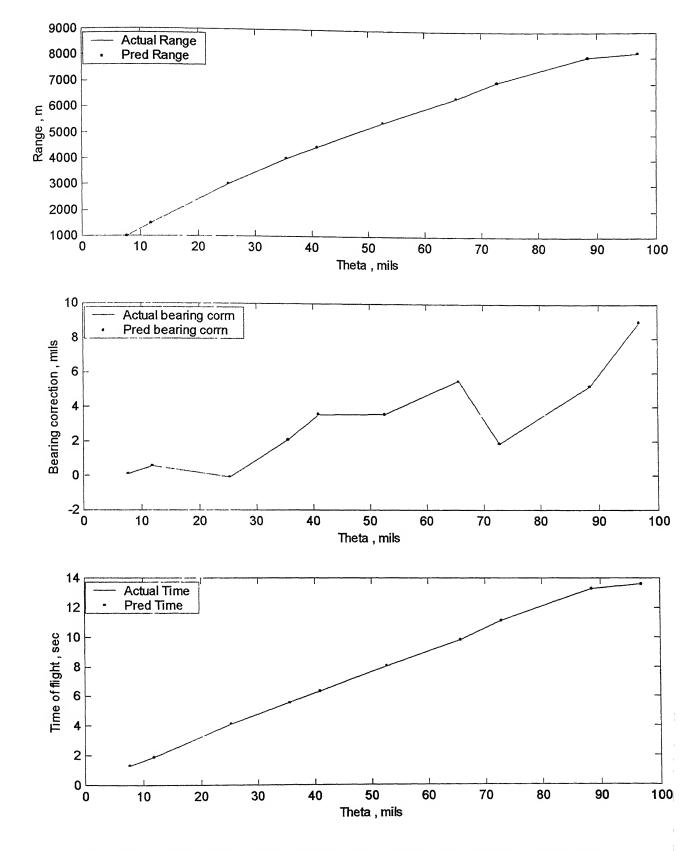


Fig. 4 Comparison of Actual and Predicted range, Bearing Correction and Time of Flight with Theta for Model 1

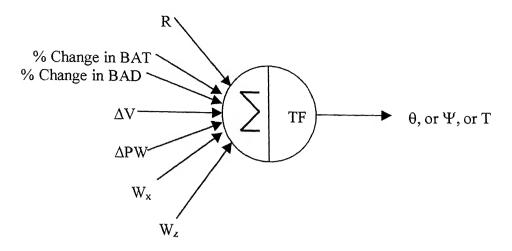


Fig.5 Schematic Representation of FFNN For model 2

Before attempting the above model, it was decided to first study simpler modelling problem. The number of inputs to the network were restricted to only two: the desired range and one from BAT, BAD, ΔV , ΔPW , W_x , W_z . Fig.6 shows schematic of six such submodels studied. It may be noted that, as in Model 1, the BAT and BAD are given in percent change from nominal values, and the ΔV , ΔPW are given in terms of difference from the corresponding nominal values.

The results for Model 2 are shown in Table 2 and Fig.7. The predicted θ , Ψ , T compare well with the actual values, the prediction being marginally better for the lower value of θ . One explanation for such observed behaviour is the fact that at lower end of θ , the range obtainable is more sensitive to variation in θ ; typically, increase of 1 mil in θ results in range increasing by 134 m for a nominal value of $\theta = 0.7$ mil, but at nominal value of $\theta = 802.3$ mils, 1 mil increase in θ would result in range increasing by only by 3.2m. Notwithstanding this sensitivity of range on nominal value of θ , the predicted values by Model 2 are quite acceptable for the whole range of θ values.

Model 2a

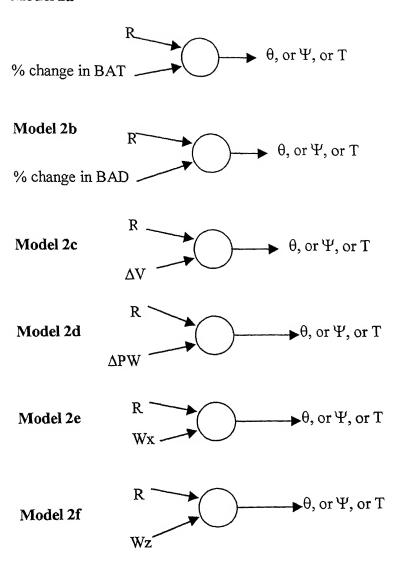


Fig.6 Schematic Representation of FFNN for sub models of Model 2

Table 2. Model 2: Comparison of Actual and Predicted Firing angle (θ) , Bearing correction for Drift (Ψ) and Time of flight (T) for ambient atmospheric conditions, shell weight and muzzle velocity considerations.

Range	θir	ı Mils	Ψi	n Mils	Ti	n sec
in m	Actual	Predicted	Actual	Predicted	Actual	Predicted
20100	509.10	508.85	-0.08	0.10	55.50	57.20
22800	738.60	744.50	38.60	37.75	74.90	74.80
23000	774.60	773.00	36.95	37.10	77.90	76.76
14000	233.50	234.00	4.10	4.88	30.30	31.20
10000	125.50	124.40	10.15	10.50	18.00	17.61
15100	272.50	273.30	15.04	15.50	34.20	34.29
12600	189.70	191.00	17.85	18.80	25.70	25.53
4100	36.50	36.40	0.0	0.10	5.80	5.60
1100	8.50	8.70	-0.10	-0.23	1.40	1.31
200	1.50	1.62	0.15	0.20	0.20	0.32

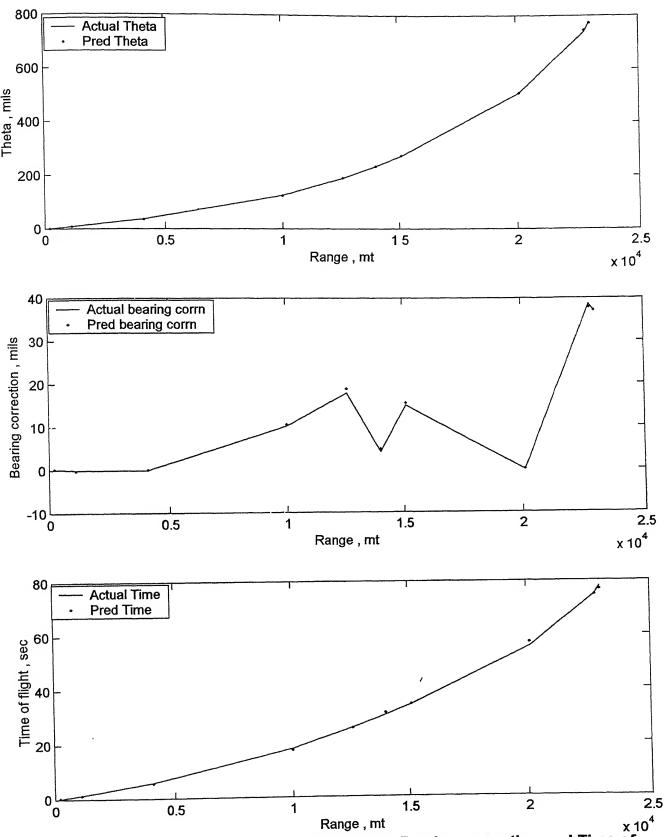


Fig. 7 Comparison of Actual and Predicted Theta, Bearing correction and Time of flight varying Range, V, PW, BAT, BAD, W_x and W_z for Model 2.

The results for the submodels Model 2a to Model 2f are discussed next. It was realized that all the submodels could be viewed as a special case of model 2. It would be, therefore, of interest to see how the results from the submodels compare with these from Model 2 by keeping R and only one of the input variables, corresponding to the submodel, nonzero and the rest of the input variables to zero. For example, for submodel Model 2a, the Model 2 would have R and % change in BAT as nonzero inputs, and the rest of these, i.e., % change in BAD, ΔV , ΔPW , W_x , and W_z equals to zero during the prediction phase. The results so obtainable via submodels and via Model 2 are compared in Table 3 - 8 and Figs. 8 - 13. The results as a special case of Model 2 corresponding to the submodels are given under the heading 'Special - Model 2'. It is noted that, as expected, the results via the submodels are uniformly better than those obtained as special case of Model 2.

4.5 Model 3

It is of interest to develop a model that can yield standard range (X) obtainable under standard conditions - temperatures and density corresponding to sea level values in standard atmosphere, no head/tail wind, shell having standard muzzle velocity and weight. The data assumed to be available for such modelling is the measured range (R) for existing ambient temperature, density, head/tail wind, muzzle velocity and shell weight. Two distinct approaches are used and the models, named model 3A and model 3B, have been developed for the purpose of predicting standard range.

Model 3A

The standard range differs from the non-standard range due to the effect of i) variations in atmospheric temperature and density, ii) amount of head/tail wind, iii)

Table 3. Model 2a: Comparison of Actual And Predicted Angle of Firing (θ), Bearing Correction for Drift (Ψ) and Time of Flight (T) for Ballistic air temperature (BAT) Consideration.

Range		θ in Mils			Ψ in Mils			T in sec	
ii E	Actual	Model 2a	Special - Model 2	Actual	Model 2a	Special - Model 2	Actual	Model 2a	Special - Model 2
20100	509.10	509.10	510.20	17.20	17.20	17.50	55.50	55.50	57.20
22800	738.60	740.30	735.02	25.70	25.48	24.90	74.90	75.20	73.35
23000	774.60	773.00	765.57	27.60	28.20	26.60	77.90	78.00	77.37
14000	233.50	234.00	232.70	8.90	66.8	9.30	30.30	30.30	30.54
10000	125.50	126.01	124.01	5.20	5.17	5.28	18.00	18.00	18.15
15100	272.50	273.30	270.82	10.10	10.30	10.61	34.20	34.23	33.67
12600	189.70	189.04	190.50	7.60	7.60	7.90	25.70	25.60	26.30
4100	36.50	36.40	36.11	1.50	1.53	1.41	5.80	5.76	6.01
1100	8.50	8.70	8.80	0.30	0.30	0.35	1.40	1.40	1.45
200	1.50	1.53	1.62	0.10	0.12	0.12	0.20	0.21	0.25

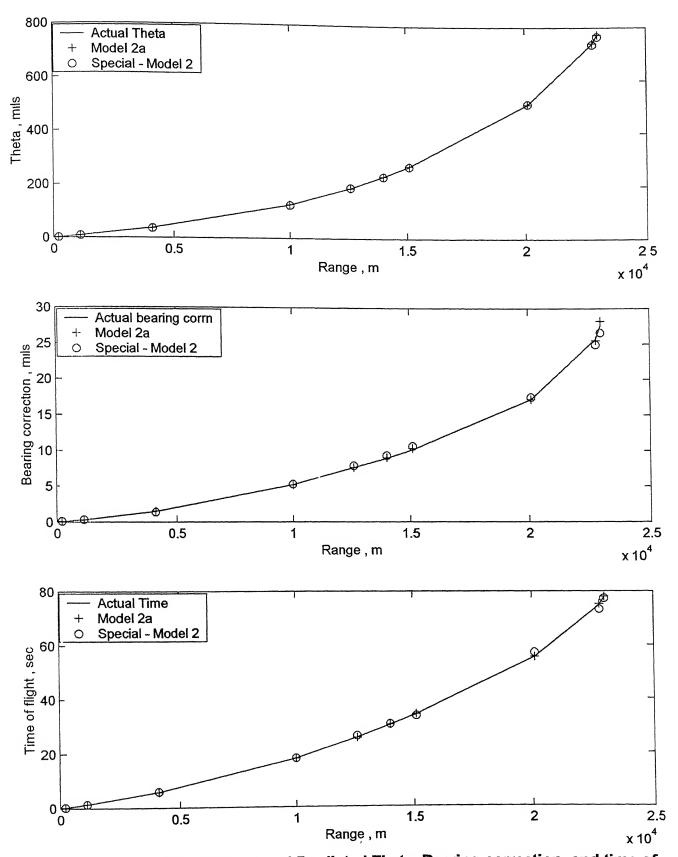


Fig. 8 Comparison of Actual and Predicted Theta, Bearing correction, and time of flight for varying Range and BAT.

Table 4. Model 2b: Comparison of Actual And Predicted Angle of Firing (θ), Bearing Correction for Drift (Ψ) and Time of Flight (T) for Ballistic air density Consideration.

Range		θ in Mils			Ψ in Mils			T in sec	
in m	Actual	Model 2b	Special - Model 2	Actual	Model 2b	Special - Model 2	Actual	Model 2b	Special - Model 2
20100	509.10	509.10	510.20	17.20	17.22	17.50	55.50	55.50	57.20
22800	738.60	741.30	735.02	25.70	25.40	24.90	74.90	75.00	73.35
23000	774.60	773.20	765.57	27.60	28.00	26.60	77.90	78.00	77.37
14000	233.50	233.60	232.70	8.90	8.91	9.30	30.30	30.30	30.54
10000	125.50	125.01	124.01	5.20	5.16	5.28	18.00	18.00	18.15
15100	272.50	273.43	270.82	10.10	10.30	10.61	34.20	34.23	33.67
12600	189.70	189.04	190.50	7.60	7.50	7.90	25.70	25.60	26.30
4100	36.50	36.45	36.11	1.50	1.53	1.41	5.80	5.76	6.01
1100	8.50	8.80	8.80	0.30	0.32	0.35	1.40	1.40	1.45
200	1.50	1.53	1.62	0.10	0.15	0.12	0.20	0.21	0.25

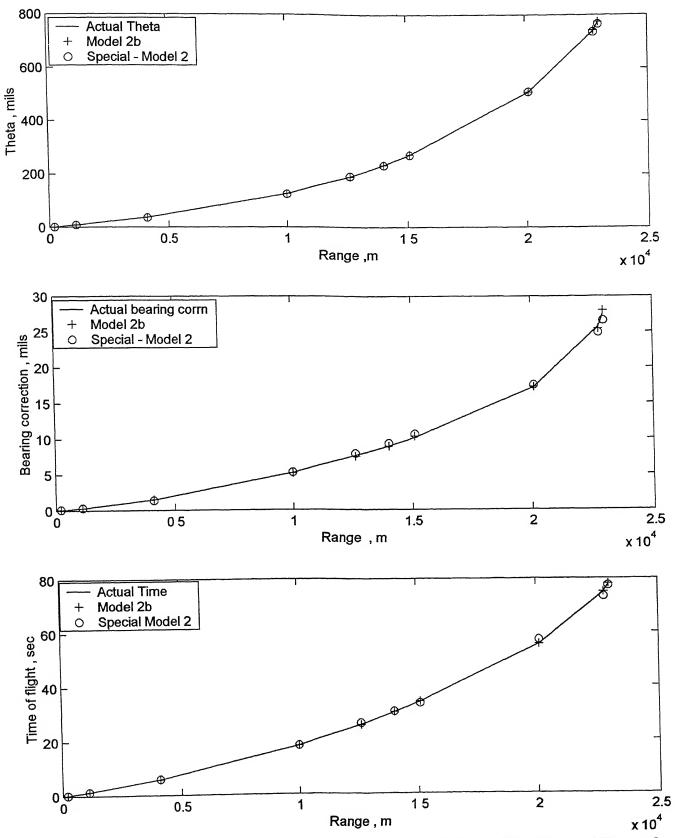


Fig. 9 Comparison of Actual and Predicted Theta, Bearing correction and Time of flight for varying range and BAD.

Table 5. Model 2c: Comparison of Actual And Predicted Angle of Firing (θ), Bearing Correction for Drift (Ψ) and Time of Flight (T) for Velocity Consideration.

Range		θ In Mils			Ψ In Mils			T in Sec	
in m	Actual	Model 2c	Special - Model 2	Actual	Model 2c	Special - Model 2	Actual	Model 2c	Special - Model 2
20100	509.10	509.10	510.20	17.20	17.26	18.10	55.50	55.46	60.20
22800	738.60	740.30	735.02	25.70	25.80	24.59	74.90	75.02	70.35
23000	774.60	773.00	765.57	27.60	28.50	25.80	77.90	78.20	77.37
14000	233.50	234.00	232.70	8.90	9.01	9.80	30.30	30.31	30.54
10000	125.50	126.01	124.01	5.20	4.97	5.28	18.00	18.30	18.15
15100	272.50	273.30	270.82	10.10	10.40	10.61	34.20	34.35	33.67
12600	189.70	189.04	190.50	7.60	7.38	7.90	25.70	25.70	26.30
4100	36.50	36.40	36.11	1.50	1.61	1.31	5.80	5.76	6.01
1100	8.50	8.70	8.80	0.30	0.35	0.40	1.40	1.37	1.45
200	1.50	1.53	1.62	0.10	0.15	0.20	0.20	0.22	0.25

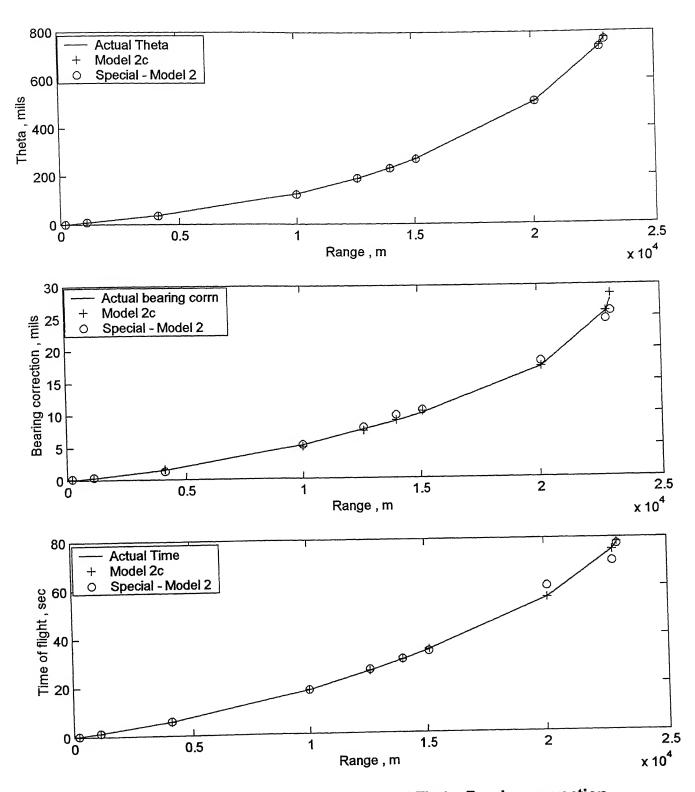


Fig. 10 Comparision of Actual and Predicted Theta, Bearing correction, and Time of flight for varying Range and V.

Table 6. Model 2d: Comparison of Actual And Predicted Angle of Firing (θ), Bearing Correction for Drift (Ψ) and Time of Flight (T) for Projectile weight Consideration.

Range		θ in Mils			ψ in Mils			T in sec	
in m	Actual	Model 2d	Special - Model 2	Actual	Model 2d	Special - Model 2	Actual	Model 2d	Special - Model 2
20100	509.10	509.12	510.20	17.20	17.25	17.50	55.50	55.50	57.20
22800	738.60	740.30	735.02	25.70	25.30	24.90	74.90	75.10	74.50
23000	774.60	773.25	765.57	27.60	28.00	26.60	77.90	78.00	77.37
14000	233.50	233.40	232.70	8.90	8.90	9.30	30.30	30.31	30.54
10000	125.50	125.60	124.01	5.20	5.16	5.28	18.00	18.10	18.15
15100	272.50	272.30	272.82	10.10	10.30	10.61	34.20	34.23	33.67
12600	189.70	189.80	190.50	7.60	7.70	7.90	25.70	25.60	26.30
4100	36.50	36.40	36.11	1.50	1.53	1.41	5.80	5.70	6.01
1100	8.50	8.80	8.40	0.30	0.32	0.35	1.40	1.40	1.45
200	1.50	1.52	1.60	0.10	0.15	0.12	0.20	0.21	0.25

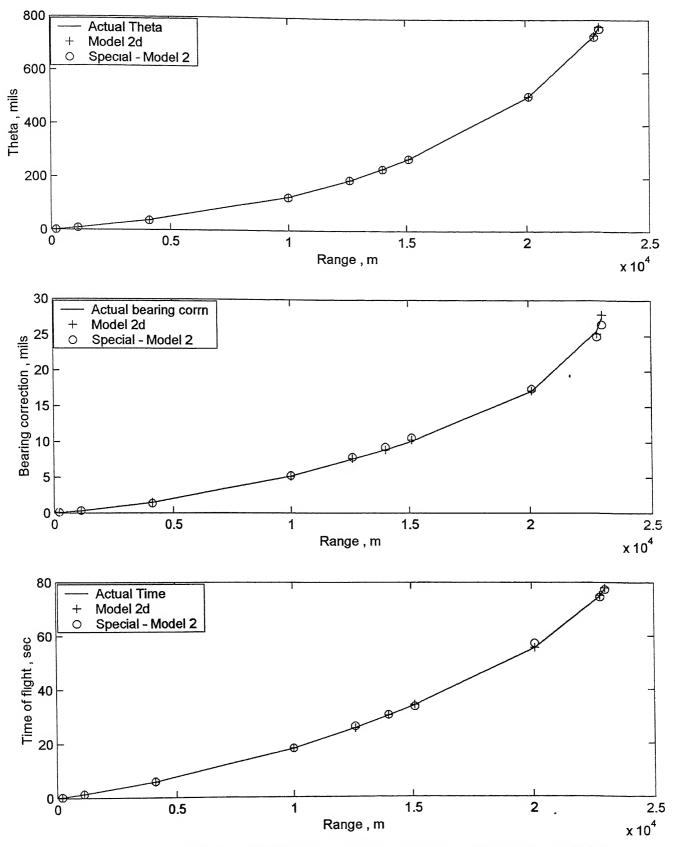


Fig. 11 Comparison of Actual and Predicted Theta, Bearing correction, and time of flight for varying Range and PW.

Table 7. Model 2e: Comparison of Actual and Predicted Angle of firing (θ), Bearing Correction for drift (Ψ) and time of flight (Τ) for head/tail wind consideration.

Dongo in		A in Mils			Y in Mils			T in sec	
m m	Actual	Model 2e	Special -	Actual	Model 2e	Special - Model 2	Actual	Model 2e	Special - Model 2
20100	509.10	510.10	510.20	17.20	17.26	18.10	55.50	55.50	56.20
22800	738.60	735.10	736.02	25.70	25.70	24.59	74.90	74.90	73.35
23000	774.60	774.00	765.00	27.60	27.70	25.80	77.90	77.90	77.37
14000	233.50	233.50	232.50	8.90	8.90	9.60	30.30	30.20	30.54
10000	125.50	125.50	124.00	5.20	5.15	5.20	18.00	18.08	18.15
15100	272.50	272.30	270.82	10.10	10.20	10.50	34.20	34.35	33.67
12600	189.70	189.40	190.50	7.60	7.40	7.60	25.70	25.67	26.30
4100	36.50	36.54	36.10	1.50	1.41	1.41	5.80	5.76	6.01
1100	8.50	8.47	8.70	0.30	0.35	0.40	1.40	1.38	1.45
200	1.50	1.53	1.60	0.10	0.15	0.18	0.20	0.19	0.25

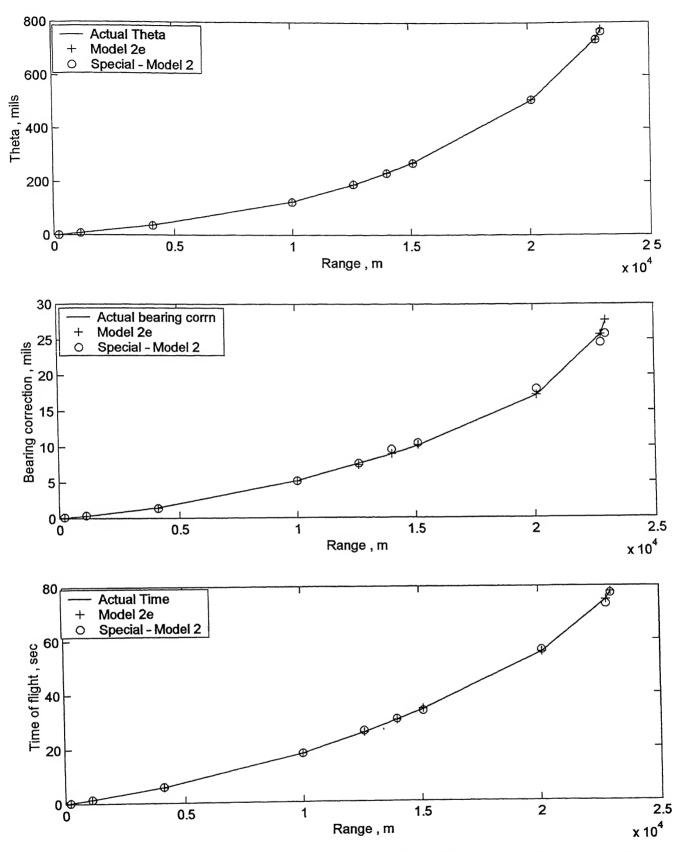


Fig. 12 Comparison of the Actual and Predicted Theta, Bearing correction, and Time of flight for varying Range and $\mathbf{W}_{\mathbf{x}}$.

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Table 8. Model 2f: Comparison of Actual and Predicted Angle of Firing (θ), Bearing Correction for Drift (Ψ) and Time of Flight (T) for crosswind consideration.

				Γ	T	Τ	Γ		,		
	Special - Model 2	56.20	73.35	77.37	30.54	18.15	33.67	26.30	6.01	1.45	0.25
T in sec	Model 2f	55.56	74.49	76.90	30.32	18.18	34.05	25.70	5.46	1.48	0.20
	Actual	55.50	74.90	77.90	30.30	18.00	34.20	25.70	5.80	1.40	0.20
	Special - Model 2	0.07	38.20	37.17	4.22	10.32	15.40	17.70	0.01	0.17	0.15
Ψ in Mils	Model 2f	80.0	38.75	37.07	4.20	10.20	15.05	17.75	0.01	0.15	0.13
	Actual	80.0	38.60	36.95	4.10	10.15	15.04	17.85	0.0	0.10	0.15
	Special - Model 2	509.20	736.52	770.00	232.50	125.00	271.82	190.10	36.40	8.60	.1.56
θ in Mils	Model 2f	200.00	737.10	774.00	233.50	125.50	272.30	189.40	36.54	8.45	1.53
	Actual	509.10	738.60	774.60	233.50	125.50	272.50	189.70	36.50	8 .50	1.50
Range	in m	20100	22800	23000	14000	10000	15100	12600	4100	1100	200

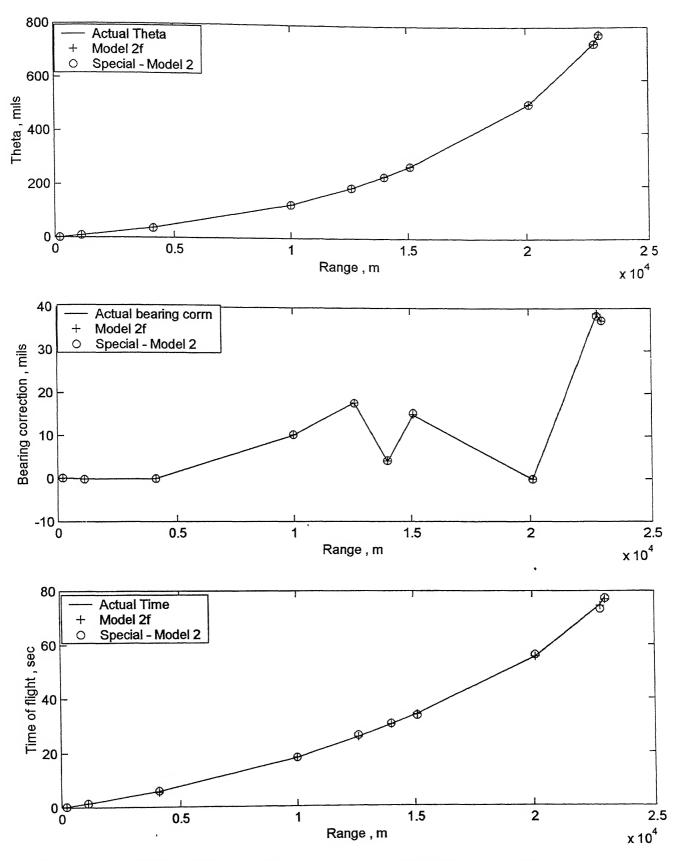


Fig. 13 Comparison of Actual and Predicted Theta, Bearing correction and Time of flight for varying Range and W_z.

variations in muzzle velocity and shell weight from the nominal values. If one could evaluate sensitivity coefficients that estimate how much the range varies per unit change in each of these, then one can calculate the standard from the non-standard range as follows:

$$X = R - \left(\frac{\partial R}{\partial T}\right) \Delta T - \left(\frac{\partial R}{\partial \rho}\right) \Delta \rho - \left(\frac{\partial R}{\partial W_{X}}\right) \Delta W_{X} - \left(\frac{\partial R}{\partial V}\right) \Delta V - \left(\frac{\partial R}{\partial PW}\right) \Delta PW$$
 (4.2)

where X is the standard range, R the non-standard range, $\left(\frac{\partial R}{\partial T}\right)$, $\left(\frac{\partial R}{\partial \rho}\right)$, $\left(\frac{\partial R}{\partial W_{x}}\right)$,

 $\left(\frac{\partial R}{\partial V}\right)$ and $\left(\frac{\partial R}{\partial PW}\right)$ are, respectively, the sensitivity coefficients with respect to temperature, density, head/tail wind, muzzle velocity and shell weight. ΔT = T - T_o , $\Delta \rho$ = ρ - $\rho_o, \Delta V = V$ - $V_o, \Delta PW$ = PW - $PW_o,$ where $T,\,\rho,\,V,\,PW$ are the values of temperature, density, muzzle velocity and shell weight at time of firing, and To, po are the sea level standard values, Vo and PWo are the nominal value of muzzle velocity and shell weight. The W_x is the value of head or tail wind (W_x is positive for tail wind and negative for head wind). To estimate sensitivity coefficients, five separate neural models (shown in fig.14) were developed. The methodology used is based on the Delta method proposed in ref. [8,13] for estimating aircraft stability and control derivatives from the flight data. The derivatives (sensitivity coefficients $\left(\frac{\partial R}{\partial T}\right)$, $\left(\frac{\partial R}{\partial \rho}\right)$, etc.) can also be estimated by using the Delta method. Here the FFNN is trained to map one of the input variables from T, ρ , Wx, V, PW to the output variable range(R). The network input is now given a small perturbation in both increasing and decreasing directions. Such a modified input file is now presented to the trained network to predict the Range, R at its output node. The difference in the predicted value of the range from the value predicted for the original value of the input is attributed to the perturbation of the chosen input variable. The difference so calculated in the value of range divided by the perturbation value introduced in the input variable yields the corresponding sensitivity coefficients. For example, to estimate $\left(\frac{\partial R}{\partial T}\right)$, the temperature T is varied to $T + \Delta T$ and $T - \Delta T$ and the corresponding predicted range R^+ and R^- are recorded. Then

 $\left(\frac{\partial R}{\partial T}\right) = \frac{R^+ - R^-}{2\Delta T}$. For the purpose of illustration, non-standard range corresponding to standard range of 20000 m was calculated for various combinations of T, ρ , W_x, V and PW. A set of 15 such data was used to train the five neural networks having non-standard range as the output and one out of T, ρ , W_x, V, PW as the input. The trained network was used to estimate the five required sensitivity coefficients; one from each of the networks shown in fig.14. Finally, the standard range is calculated by using Eq. 4.2. A comparison of predicted and actual standard range is given in Table 9. Table 9 lists the non-standard range along with the sensitivity coefficients. Table 9 shows that the standard range estimates via sensitivity coefficients compare well with the actual standard range. However, this approach is a round about way of predicting standard range, and, therefore, a more direct method would be highly desirable. This search for a direct method led to the following model.

Model 3B

Model 3B has two versions, named Model 3B-1 and Model 3B-2 that were studied. Model 3B-1 is identical to Model 1, but it is used in a special way for estimating standard range. Like Model 1, output of the network is range R, which is mapped to θ ,

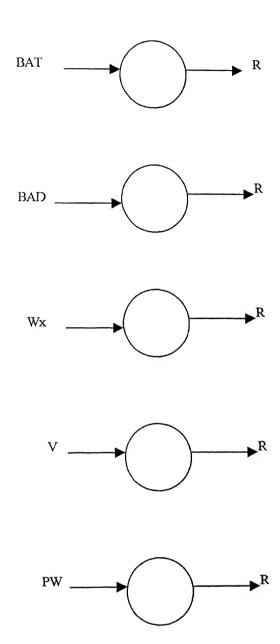


Fig.14 Schematic of Neural Models for Estimating Sensitivity Coefficients

Table 9. Model 3A: Comparison between actual and calculated range at standard atmospheric conditions.

	×															
Diff. Bet.	Actual &	-11.00	-0.94	-0.60	-4.59	-4.10	-6.61	-1.98	-2.47	1.72	1.39	-2.58	-14.90	-2.72	-4.11	-1.34
Calculated	X in m	20011.0	20000.9	20000.6	20004.5	20004.1	20006.6	20001.9	20002.4	19993.2	19998.6	20002.5	20014.9	20002.7	20004.1	20001.3
Actual X	E E	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0	20000.0
AR.	ØPW	45.00	45.01	42.04	45.00	45.01	45.00	44.97	44.99	44.99	42.53	45.01	42.54	43.88	45.00	44.96
AR.	<i>φ</i>	-106.86	-109.08	-107.19	-109.08	-107.42	-107.15	-109.10	-108.44	-103.30	-109.20	-109.10	-107.71	-109.18	-107.77	-109.10
AR.	<u>TC</u>	-0.31	0.23	-1.09	0.15	-0.92	-1.04	0.19	-0.13	-1.39	0.26	0.19	-0.34	0.26	-0.75	0.20
AR.	$\frac{\partial W_{X}}{\partial X}$	20.80	20.80	20.80	20.80	20.80	20.80	20.79	20.80	20.80	20.64	20.80	20.75	20.80	20.79	20.69
æ	$\overline{\partial V}$	27.89	27.90	27.90	27.91	27.90	27.87	27.90	27.91	27.90	27.90	27.90	27.90	27.86	27.90	27.90
R in m		19605.1	20522.3	20319.3	20336.4	20430.0	19613.1	20264.8	19966.1	19436.4	19776.4	20224.1	19324.0	20593.9	19878.9	19945.6

 ΔV , %BAT, %BAD, ΔPW and Head/tail wind (W_x). However, mapping of the inputs to bearing correction Ψ and time of flight T is not required as done for Model 1. The network is trained on randomly selected 40 data taken from the range table. Now, the trained network is used to predict standard range for each of the firing angle θ by setting $\Delta V = \Delta PW = \%BAT = \%BAD = W_x = 0$. The standard range for various value of θ so obtained is given in table 10.

Model 3B-2 is similar to the Model 3B-1 except that instead of ΔV and ΔPW , percent change from the nominal value of the muzzle velocity and the shell weight were used as the input variables. The trained network was again used to predict standard range for various firing angles by putting all variables except θ to zero. The results are shown in Table 10.

In Table 10 and Fig.15, the predicted standard R via Model 3B-1 and Model 3B-2 are compared with that from the range table. Though both the models yield standard R which compares well with that given by the range table, it is observed that the Model 3B-2 gives relatively better results compared to Model 3B-1. Also, it may be noted that predictions for standard range are relatively better for lower values of θ , i.e., there is slight decrease in prediction accuracy of standard R as θ increases.

It is emphasized that both options of Model 3B are more suitable and straightforward to use for real life applications. In contrast, model 3A requires multiple networks to be used and calculation of the standard range using results from these networks.

Table 10. Comparison of Actual Range at standard condition for Different types of model.

heta in	R-non	X-standard	X- Model	X- Model
degree	standard	in m	3B-1 in m	3B-2 in m
	in m			
25.41	18922.00	19100.00	19107.00	19101.00
25.72	19315.00	19200.00	19205.00	19199.00
26.03	18921.00	19300.00	19304.00	19298.00
26.34	19439.00	19400.00	19404.00	19399.00
26.66	19688.00	19500.00	19503.00	19498.00
26.98	19097.00	19600.00	19602.00	19598.00
27.30	20226.00	19700.00	19701.00	19696.00
27.62	19900.00	19800.00	19800.00	19796.00
27.96	19442.00	19900.00	19900.00	19896.00
28.29	19996.00	20000.00	20001.00	19997.00
28.64	19861.00	20100.00	20101.00	20097.00
28.98	19991.00	20200.00	20201.00	20197.00
29.33	20545.00	20300.00	20302.00	20299.00
29.69	20667.00	20400.00	20402.00	20399.00
30.05	19922.00	20500.00	20502.00	20499.00
30.42	20355.00	20600.00	20603.00	20600.00
30.79	20748.00	20700.00	20703.00	20700.00
31.17	20493.00	20800.00	20804.00	20801.00
31.56	21139.00	20900.00	20903.00	20900.00
31.95	20933.00	21000.00	21003.00	21001.00
32.36	21505.00	21100.00	21104.00	21102.00
32.77	20819.00	21200.00	21204.00	21202.00
33.18	21467.00	21300.00	21303.00	21301.00
33.62	21531.00	21400.00	21403.00	21402.00
34.05	21678.00	21500.00	21503.00	21502.00
34.50	21394.00	21600.00	21602.00	21602.00
34.97	21627.00	21700.00	21701.00	21701.00
35.44	21738.00	21800.00	21800.00	21800.00
35.93	21625.00	21900.00	21898.00	21898.00
36.44	22254.00	22000.00	21997.00	21998.00
36.96	22141.00	22100.00	22095.00	22096.00
37.50	22003.00	22200.00	22192.00	22193.00
38.07	22370.00	22300.00	22291.00	22292.00
38.67	23179.00	22400.00	22390.00	22391.00
39.30	22571.00	22500.00	22488.00	22490.00
39.99	22071.00	22600.00	22590.00	22591.00
40.73	22452.00	22700.00	22692.00	22693.00
41.55	23353.00	22800.00	22796.00	22797.00
42.46	23171.00	22900.00	22903.00	22902.00
43.59	22827.00	23000.00	23021.00	23017.00

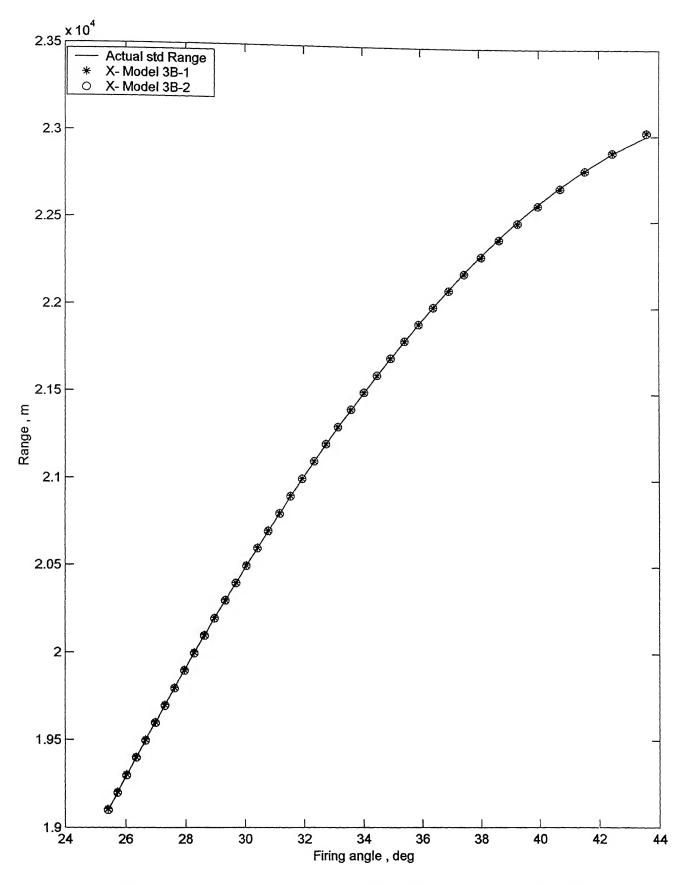


Fig. 15 Comparison of Actual and Predicted Standard Range for different types of model

CHAPTER 5

CONCLUSION

5.1 Conclusions

The validity of the neural modelling is demonstrated for three different applications relevant for artillery shells. A set of available firing data in terms of range, firing angle, shell weight, muzzle velocity, existing atmospheric conditions like temperature, density, head/tail wind, cross wind, time of flight, bearing correction are required to train the network with suitable input-output samples: which of these measured variables would form the inputs and the outputs is decided by the purpose of the neural model. In particular, for three distinct applications, a neural model has been identified and validated for B-Shell data. The results for all the models compare well with the known results. The strength of the neural models lies in the fact that once the network is trained, it can be used for on-line applications on the field of action — to predict the range for chosen angle of firing or to predict the firing angle for desired range, under the prevailing atmospheric conditions and for known shell weight and muzzle velocity.

The conventional approach, i.e., the mathematical models such as in-vacuo trajectory model, modified point mass model, six-degree-of-freedom model require knowledge of all the forces and moments acting on the shell. Evaluation of forces and moments, in turn, require aerodynamic coefficients as inputs and this fact limits the accuracy of predictions because the reliability of available estimates of these coefficients is not always high. In contrast, the proposed neural models do not require any mathematical model or its solution. This implies that the neural models do not require estimates of aerodynamic coefficients. Furthermore, if the neural network is trained on

the real data, it will automatically account for the initial conditions in an implicit way. But the mathematical models have no provisions to account for initial conditions such as gun jump and throw-off.

5.2 Suggestions for Future work

- 1) The training of the neural network depends on the architecture of the FFNNs, the activation function used by the neurons and the values selected for the tuning parameters. From the neural network point of view, lot of scope exists to explore and experiment with new evolving schemes and methodologies for improving the input-output mapping.
- 2) The present work has used the firing tables provided by ARDE, Pune. An attempt should be made to seek real firing data and validate the present models for such data. Using real data, it will be of interest to predict range for known firing angle, or to predict firing angle required for desired range using the mathematical models like the modified point mass model or six-degree-of-freedom model and also from the proposed neural Model 1 or Model 2. A comparison of results from mathematical models and neural models would show relative reliability of the predicted value for real life applications.
- 3) The data set supplied by ARDE, Pune is valid for weighted value of the head/tail wind and cross wind. This is an approximation to varying wind conditions at different altitudes through which the shell passes. It may be worthwhile to search for a way to account for varying wind conditions. The same comment also applies for finding a way to account for varying temperature and density conditions.

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Appendix A

Table F(i)

CHARGE 9-SHELL 77B Basic Data

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Altinude	1, 5	1 kox Beluse: Nux	H.,	百三	1	0-	999	0,00,0		,:::-	77777	નંતનંદોન	44444	4 4*A 4 N	યેયેયેઠે
	4		(1 kg 16 _k)	P. P.	<u> </u>	0	o'o'o o	00000	a c	,		બદાબંલ ા 	ოძოძ. 	4 4 4 4 vi	<i>ininioe</i>
	3	r.S. S.Z.c.	7	incresse	2	7	21.0.1.	51.1.5	2 6	44444	64444 00040	4 ~. ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	6,6,6,6,6,6,6,6,6,6,6,6,6,6,6,6,6,6,6,	6.9 -7.1 -7.3 -7.7	2,8 % % 2,1 % % % 5,4 %
	2	1 Mussic Mussic Vei∞no	(1 8/8 1/2)	Derrease increase	2	J.	시작 0.다	2.1.0.2.2	77	34255	33.7	25.25.8 5.22.08	5.0 6.0 6.4 6.4 6.4	6.8 7.2 7.4 7.6	2.8 8.0 8.2 8.4 8.4 8.4
	-		Rænge		3	8	8888	8888	8 5	38888	2800	2208 2208 2488 2588 2588	2,200 2,200 2,200 3,000 3,000	3200 3200 3300 3400 3500	3600 3700 3800 3900 4000
						1	•.								
	10	Correction to Correction	Height of	Sown 10M		. אוריסק									
	0.	***	for 1 kmo:	<	(PC A B!)	, Ju	8855	ie ee8	ය ස	225	ខ ខន្ន	វន្ត នូននៃន	38 8882	66 668	8 8888
	3	Correction	to la Bestring	for dark	(A.A)	mlL .	977-	:- nnn	เป็นไ	પ્ <i>યં ત</i> ં ત	יט אאאמי			2222	12 6527
			. ـ - ـ ـ د ب	ㅡ 枟.	_	S	-: ci 4: ^	10 600	-11	44100	6. 1222	20.000	16 66 66 16 70 86	74 444 747	5.0 5.1 5.3 5.3 5.3 5.3 5.3

12.6 15.5 15.2 16.1

2500 2500 3000 3000 3000 3000

22222 88888

328 328 338 348 358 358

2883.

Table F(i)
CHARGE 9-SHELL 77B
Basic Dax
Altitude Sea Level

	10	Correction to to Corrector to change Height of Burst by Down 10M	DOINES		•						
	6	Correction to Bearing for 1 knot cross wind $\Delta_C A_B / \lambda$	ri.	00000	:=2;2;2	55554 	44 4 5 S S S S S S S S S S S S S S S S S	21. 31. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	71.88	ei ei 68 64	77778
	∞	Corrections to Bearing for druli	_ _	22 33 47.1 2 2 3 4 7.1	7:31 8:30 9:00	20 20 21 21 21	22222	. 228 226 27 27	3.0228		3.6 3.6 3.7.
	ĵ	Time ं (१)	1 1	5.8 6.1 6.3 6.4	6.6 6.5 7.1 7.3	7.5 7.5 8.0 8.2	88.3 7.8 9.1 9.1	9.3 9.5 9.8 10.0	10.2	11.2	1272
Sea Level	9	Fork	15		some story bred story from		2000 POS (POS (POS)			000	ипппп
Allulade Sea	5 1	Effect on Range for increase of 1 mil in Firing Table elevation (AgrX/)	M	93.0 92.0 91.1 90.3 89.2	88.3 87.6 85.9 84.9 8	83.8 83.1 82.2 81.5 80.4	79 6 78 7 77 9 77 9	75.4 74.7 73.8 73.2 72.3	71.4 70.8 69.9 69.1 68.3	67.6 65.7 65.3 64.8	63 9 63 1 62 4 61.7 60 9
न्त		Correction 1 to Fuze 1 Setting to change 1 Height of 1 Burst by 1 Down 10M	4			<u></u> -					
	٠-،	Fuze	,				to the second to have any underlangue.				
	- ·	Firing Table clevation	i, 3	36.5	44444 644444	47.8 49.0 50.3 51.5 52.7	%%%%% %%%%% .1.8.8.1.0	50.7 65.7 85.1 8	67.2 63.6 70.0 71.5	74.4 77.4 78.9	82.0 83.6 85.2 86.8 88.4
		Series S	٠ ۲	0017 0017 0017 0017 0017 0017 0017	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	25 55 55 55 55 55 55 55 55 55 55 55 55 55	36 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	88888	888 888 888 888 888 888 888 888 888 88	នុត្តក្នុន្ត	15 15 15 15 15 15 15 15 15 15 15 15 15 1

Table F(ii) CHARGE 9-SHELL 778

Corrections to range for non-standard conditions $\Delta_C X$

-	2	3	41	Altitud	Altitude Sea Level 5 6 1	rel 7	00	6	01	.=
•	Z Z	1 M/S Muzzle Velocity		1 Knoc Ballistic Wind	Ballus Temp	1 % Ballistic Aur Temperature	Bal	1% Ballistic Density of Dees	£.*	Projectic Weign:
Range	(134)	(1 x/s 1/ ₆)	(1K	(1 KT H'B)	(125 TB	TB)	100 P	Lecundent	<u>.</u>	/ التاسي _ا /
(X)	Decrease (-)	Increase (+)	至	[基] (英)	-	Occease Increase	Decrease (-)	incre25c (+)	1 <u>0</u>	(-) (-)
	Σ	×	X	. M	Σ	×	Σ	X	ブ	×
014 4 2000 4400 6500 6500 6500 6500 6500 6500 6	73 2 2 2 2 2 2	8.6.6.6.6.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.	01. L. L. 00	6 7 7 8	-1.6 -1.7 -1.8 -1.9	+1.6 +1.7 +1.8 +1.9 +2.0	6 4 1 1 1 8 4 1 4 4 4 4 4 4 4 4 4 4 4 4 4	7.7 7.3 8.1 8.4	*****	77777
4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	9.6 9.8 10.0 10.2	-9.7 -9.9 -10.0 -10.2	∞ ≈ 0 0 0 0 i	٠ ٠٠٠٠ ٠٠٠ ٠٠٠ ٠٠	<u> </u>	+ + + + + + + + + + + + + + + + + + +	-88- -99- -100- -104-	8.8 9.2 9.6 10.0	## # ###	nann
5200 5300 5400 5500	10.5 10.7 10.9 11.0	-10.6 -10.7 -10.9 -11.1	22222	1.	.26 .27 .28 .30	+26 +27 +28 +28 +29	-10.8 -11.2 -12.1 -12.6	10.8 11.2 11.6 12.1 12.5	251114	2222
5600 5700 5900 5900	11.3	-11.4 -11.6 -11.7 -11.9	<u> </u>	<u> </u>		+3.1 +3.2 +3.5 +3.5 +3.6	-13.0 -13.5 -13.9 -14.4	12.9 13.9 14.3 14.8	77777	23222
6238 6388 6488 6588	222322	-122 -124 -125 -127	47779	4.11.14.4	4444 10000	##### 7.001.E	-15.4 -15.9 -16.9 -17.4	15.3 16.3 16.3 16.8	77700	ដល់ដាប់ប
6500 6700 6800 6800 7000	13.2 13.2 13.4 13.4	-13.4 -13.4 -13.4	7.11 8.11 9.11 9.11	7.1.1. 8.1.1. 9.1.	4444 40000	44144 461.80	-180 -185 -191 -196 -202	17.9 18.4 19.0 19.5 20.1	20214	BBHBH
7100 7200 7300 7500	13.8	-13.7 -14.0 -14.1 -14.3	777	, 20 , 20 , 21 , 21 , 21	2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2	+5.1 +5.3 +5.4 +5.6 +5.7	-20.7 -21.3 -21.9 -21.9 -21.9	20.6 21.2 21.8 22.8 22.9		(Ideas
7600 7700 7800 7800 8000	144 147 148 148	-14.6 -14.6 -14.7 -15.0	22223	22422	66.1.0 66.3.7 7.7	+61 +62 +64 +664	.25.2 .25.2 .25.2 .25.2	23.5 24.1 25.4 25.4 25.0	111111111111111111111111111111111111111	00000

Table F(i)

CHARGE 9-SHELL 77B Basic Data Altitude Sea Level

Conector to change Haght of Burst by Down 10M 10 Correction roints 9 to Beaning for 1 knot Correction erross wind REBER <u> ಜನಸಭಜ</u> **#####** Correction to Bearing for drift (\$ 42) Time of flight Port S Correction Effect on to Fuze Range for Scring to increase change of 1 mill Heigh of In Finng Burst by Table [Down 10M; elevation] Effect on Range for (\$\rightarrow FS 1) (\$\rightarrow FS 1 \) (\$\rightarrow 10 MJ, \) (\$\rightarrow 10 MJ, \) Sching Fizz (FS) Finrg Table 8200 8300 8500 8500 8850 8300 8900 8900 8900 98689 98889 98889 10200 10200 10300 10400 10600 10700 10800 11000 (X)

Table F(ii)

CHARGE 9-SHELL 77B

Corrections to range for non-standard conditions $-\Delta_{\mathcal{L}}$).

Altunde Sea Level

	=	Property Transparts Wage	- ال	boreasc	×	Q√Q√∞∞ ε∕	rr998	NN444	w0101	00077	いらいかいん	かかみない	8 8 9 Q C
	10	Prox	(104	Decrease, berease	Z	တ်တဲ့လုံလ်တ	44-	かかまなむ	44444	00007	4322-	40000	90
	ی.	19. Balusuc Densiy or Drag Coefficient	(a)	Increase	33	26 6 27 3 27 9 22 6 29 2	29 9 30.6 31.3 32.0	82883 2555	37 0 37 7 38 5 39 2 40 0	44.6 44.5 53.9	445 453 472 480	48 9 49 7 50 5 51 4 52 2	82882 82882
	3	Density Cock	(1%	Decrease	×	27.5 27.5 1.35.1 2.8.5 2.9.5	301-308-308-315-329-329-329-329-329-329-329-329-329-329	35. 35. 35. 35. 35. 35. 35. 35. 35. 35.	3880	77477	15.54 15.50 15.60 15.60	-501 -510 -518 -518	\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$
Level	1 3	1 % Ballishe Air Temperature	T _B)	Occrease Increase	X	+67 +69 +71 +72 +72	+76 +78 +7.9 +81 +81	+ + + + + + + + + + + + + + + + + + +	+9.5 +9.6 +9.8 +10.0	+100 +109 +11.1	+11.5 +12.0 +12.2 +12.2	+12.7 +12.9 +13.1 +13.3 +13.5	+13.7 +13.9 +14.1 +14.3 +14.5
Sea	9	Ballis Temp	(1%T _B		Σ	-68 -70 -72 -74 -75	-7.7 -7.9 -8.1 -8.3 -8.5	2000 2000 2000 2000 2000 2000 2000	-9.7 -9.9 -10.1 -10.3	10: 109: 1111 114	-11.8 -12.0 -12.3 -12.5 -12.5	-13 0 -13 2 -13.5 -13.7 -13.9	-142 -144 -147 -14.9
Alrunde	\$	1 kno: Ballistic Winc	. H .	Tzi. (x)	M	2.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7.7	64444 00144		4444 8000-1	44144 00400	4.142.2.	244 444 544 544	8.5.5.6.6.6.6.5.5.6.6.6.5.5.6.6.6.5.5.6
	7	_ B =	(187	整	X	27 37 37 87 87 87	66666 66666	WWWWW. 4000c	8 8 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4444	25.082	20000 2000 2000	5.8 6.1 6.2 6.3
	3	1 M/S Muzzle Velocity	(1 x/s V _o)	: Increase	, M	1 -15 1 -15.2 -15.4 -15.5 -15.6	-158 -160 -161 -161	166	-17.0 -17.1 -17.1 -17.4 -17.5	-176 -17.7* -17.8 -18.0 -18.1	-18.2 -18.3 -18.4 -18.5 -18.6	-18.7 -18.9 -19.0 -19.1	-193 -194 -195 -19.6
	CI		(וא'	Doctrase (-, 1	ĭ	151 152 153 154 155	15.7 15.9 16.0 16.1	164 165 168 169	170 17.1 17.3 17.4	, 17 6 17 7 17.8 18.0 18.1	18.2 18.3 18.5 18.5	18 8 18 9 19 0 19.1	19.3 19.4 19.7 19.8
	-	Z C	3	(X)	×	8220 8320 8380 8280 8280 8280 8280 8280	88888 88888 88888888888888888888888888	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	9,869 9,760 9,860 9,800 9 9,800 9 9,800 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	10200 10200 10300 10400 10500	10600 10700 10800 10800 10900	11100 11200 11300 11400 11500	11600 11700 11800 11900
	a	*\~ 13 \~ .	75	1	1								

Table F(i)
CHARGE 9-SHELL 77B
Basic Date
Altitude Sea Level

										1
10	Correction to Corrector to change Height of Burst by Down 10M	roints			-					
6	Correction to to Bearing for 1 knot erross wind (\(\Delta_C A_B\) (\lambda_C A_B\)	E	8 9 9 9 1 1	4.4.4.6.6	41258	44 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	4.8 4.9 4.9 50	8일284	स्रह्म स्रह्म	<i>ব্য়</i> গ্রপ্থ
90	Correction: to Beanng for dark	ml.	7.1.7.2.7.7.3.3.7.5.4.8.7.5.7.5.7.5.7.5.7.5.7.5.7.5.7.5.7.5.7	7.7 7.3 7.9 8.0	88888 0.1268 7.426	888888 807.80	(, 4000 (' 4640	96 97 98 999 0.00	. 10.1 10.3 10.5 10.6	10.7
7	Time of Night (11)	S	25.22 25.05	25.7 25.0 25.0 27.0 27.0	27.3 27.6 28.0 28.3 28.3	29.3 29.3 30.0 30.3	30.7	32.5	35.3	36.5 36.5 36.5 37.2 37.2
9	Fork (/)	Έ	4444	44NNN	พพพพพ	νννον	9911199	40000	~~~~	r-r-∞∞
- S	Effect on Range for increase of 1 mul in Firing Table elevation $\left(\frac{\Delta_{EF} K}{+1}\right)$	M	36.7 35.3 35.3 94.9	333346	32.7 32.3 32.0 31.7 31.3	31.0 30.7 30.3 30.1	28 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	28.0 27.9 27.2 27.2 27.2	88888 90309	222222 34.2222 1.022
4	Correction to Fuze Setting to Setting to change Height of Down 10M, Correction Correct							-		
-		-	757 784 812 840 869	189.7 192.6 195.6 198.6 201.6	204 6 207 7 210 8 214 0	23.5 23.5 23.5 23.5 23.5	236.9 240.3 243.8 247.2 250.7	전 1 : 1 : 1 : 1 : 1 : 1 : 1 : 1 : 1 : 1	272.5 276.2 283.8 283.8	291.6 295.5 299.4 303.4
2	Finng Table clevation	E	2.5.83.8	82668	55555			`		
-		ン	250 250 250 250 250 250 250 250 250 250	2500 2727 2720 2720 2720 2720 2720 2720	13288 13288	800 800 800 800 800 800 800 800 800 800	88888	0064 270 270 2064 0064 0064 0064	244242 28888	8552 8888 8698 8698

Table F(ii)
CHARGE 9.SHELL 77B
Corrections to range for non-standard condutions $\Delta_C X$ Altitude Sea Level

	:-	1□ Projectue Wagh:	me, 1	Incresse	7	-4444	425145	7.888.55	ង់ង់ង់ង់	ត់ជំង់ង់ង	<u> </u>	អង់ង់ស់ស	ឯមម្ភម្ពុក្
	2	(6.3×	(1பக,	Increase Decrease Increase (+) (-) (+)	M	22210	::4558	887778	58827	ដដដដ	*****	22222	28833
	6	19 Ballistic Density of Drag Coefficient	D ₃)	Increase (+)	≅	57.3 58.2 59.0 59.8 60.7	61.5 62.3 63.1 63.8 64.6	65.4 66.9 67.6 63.4	69.1 706 71.3 72.0	72.7 73.4 74.1 74.7	76.1 76.8 77.4 78.1	79.4 80.0 80.7 81.3	83.2 83.2 84.5 85.3
	s	Ball Density Coeff	(1% D ₃	Doctesse (-)	Σ	58.8 596 505 513	62.1 63.8 64.6 64.6	66.2 67.0 67.7 68.5 69.3	-70.0 -70.8 -71.5 -72.7 -73.0	-73.7 -74.4 -75.1 -75.8	277. 977. 285. 295.	\$06 \$1.2 \$1.3 \$25 \$3.1	853 844 857 857 863
ser.	1 7	1 % Ballusac Air Temperature	TB)	Decrease Increase	Σ	+14.7 +14.8 +14.9 +15.1 +15.2	+153 +154 +155 +155 +155	+15 6 +15.6 +15.7 +15.7 +15.7	+15.6 +15.6 +15.6 +15.5 +15.5	+154 +154 +153 +153 +151	+150 +148 +147 +146 +145	+143 +142 +140 +138	+13.5 +13.3 +13.1 +12.9 +12.7
e Sea Lorel	9	Ballus Temp	(12TB		Σ	-153 -156 -158 -160 -161	-163 -165 -16.7 -16.7	-170 -171 -171 -172	17.3	-17.3 -17.3 -17.3 -17.2	-171 -170 -16.9 -16.8	-16.6 -16.5 -16.4 -16.3 -16.1	-160 -158 -15.6 -15.5
Almude	5	1 Knot Ballistic Wind	118)	Tan (%)	Σ	9999 9999 9999	70 77- 77- 7.5 7.5	1-1-8-8-8- 1-2-8-8-8-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-	8 8 8 8 9 7 8 8 9 1	9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.9.	-10 0 -10.2 -10.4 -10.5	-10.9 -11.0 -11.2 -11.4	-11.7 -12.1 -12.2 -12.2
	4	1 k Bal	(1KT N _B)	台	Σ	6.4 6.7 6.8 6.8	7.1 7.2 7.3 7.5	7.8 7.9 8.2 8.3	8.88.6 2.88.0 1.98.0	- 99999 907	10.2 10.2 10.4 10.5	10.0 11.0 11.4 11.4	11.7 11.9 12.1 12.2 12.2
	: 3	1 M/S Muzzle Velocity	(% 5	Increase (+)	Σ	-19.8 -20.0 -20.1 -20.2 -20.3	28.4 28.5 28.7 28.8	-20.9 -21.0 -21.1 -21.2 -21.3	-21.4 -21.5 -21.6 -21.7 -21.7	21.3 22.2 22.2 22.2 23.2 23.2 23.2 23.2	<u> </u>	វៀងងង់ង <u>់</u> ង	ង់ដង់ដង់ 2.3.3.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.
	2	No.	(14/5 1/9)	Decrease	M	888888 821.288	88888 87878	22222 22222 22222	21.5	ដូដូដូដូ	पुराध्या	ยู่ถูกก็ก็	ង្គងង្គង្គ
	_	ć	Kange	(x)	M	1218 1228 1238 1248 1248 1258	12600 12700 12800 12900 13000	13160 13380 13380 13480 13480	13600 13800 13800 14000	14200 14300 14300 14400 14500	14600 14700 14800 14900 15000	15100 15200 15300 15400 15800 15800	15600 15700 15800 15800 15900

Table F(i)

CHARGE 9-SHELL 77B Alutude Sea Level Basic Data

Corrections to range for non-standard conditions $\Delta_{\mathcal{L}} \lambda$ Table F(ii)

CHARGE 9-SHELL 77B

Allunde Sea Level

Ballistic My Profession Control of the Control of t

1% Bothstic Ato Temperature (1% TB)

| Knot Ballistic Wind | Knot'We)

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#4446

857 863 869 875 881

144 145 145 145

-126

126 132 133

44488

89.2 89.8 90.4 91.0

90 6 90 6 91.2 91.8

+113 +110 +107 +105 +102

13.8

-135 -137 -139 -141

13.5 13.7 14.1

91.5 92.1 92.7 93.3

888488 888488

.126 .126 .123 .121

153 153 153

14.5 14.9 15.1 15.3

#88811 83538

_	1												
3	S /S	Muzzle	s voj		×	22222 2225 3225	2444 2444 2444 2444 2444 2444 2444 244	24 9 25 2 25 2 25 2 3 3	x 2 2 2 2 2 2 3 2 2 1 1 1 1 1 1 1 1 1 1 1	.260 .261 .263 .263	.265 .266 .267 .268	-270 -27.1 -27.2 -27.3 -27.3	-27.5 -27.6 -27.7 -27.8 -27.8
5	-	Z ×	/w T /	<u>-</u>	Σ	2222 222 222 222 232 232 232 232 232 23	24.5 24.5 24.7 8	*22222 *6-55	¥%%%% 4%%%%%	2888 882 833 833	88888 9486 9486	27.0 27.1 27.2 27.3 27.3	27.5 27.6 27.7 27.8 27.9
				(γ)	Σ	16100 16200 16300 16400 16500	16500 16700 16800 16800 16900	17100 17200 17300 17400 17500	17600 17533 17800 17800 18000	18100 18300 18400 18500	18600 18700 18800 18900 19000	19100 19200 19300 19400 19500	19500 19700 19800 20000
15	5		-	1									
Correction		 	<u>.</u>	_	points		w + 400						
7	Correction	Bearing for I Knot	Cross wend	LIĶTIĶ"	,μ	\$2.72.82 8	%&&&&&	8.2.2.2.2	22 <u>6</u> 822	¥48;8;8;	%% <u>;</u>	88 86 80 80 88 86 80 80	.70 .70 .71 .71
٥	correction	Bearing P. J. Go		(of 41)	ήL	11.3 11.5 11.7 8	11 ° 120 122 123 124	126 127 128 130 13.1	13.5 13.5 13.8 13.8	13.9 14.2 14.2 14.4 14.5	14.7 14.8 15.0 15.2 15.3	15.5 15.6 15.8 16.0 16.1	16.3 16.5 16.7 16.9 17.0
7			42.74	Ξ	s	38.0 38.4 38.7 39.1 39.5	39 0 40.3 40.7 41.1	41.9 42.3 42.7 43.1 43.5	444 45.2 85.2 85.2	46 1 46 5 46.9 47.4 47.8	48.3 48.7 49.2 49.6 50.1	50 6 51.0 51.5 52.0 52.5	53.0 54.5 5.0 5.0 5.0
9		निर्दे		S	Έ	∞ ∞ ∞ ∞ ∞	~~~~~	00000	2222	2222	22===	33222	22277
5	Ranpe for	in Orease	amala d	(+ (1/4 AF)	×	24.5 22.2 23.9	2233 279 279	22.5 22.3 22.1 21.8 21.7	21.5 21.4 20 9 7	20 S 20 4 20 2 19.9	19.5 19.3 18.9 18.9	18 5 18 3 17.9 17.7	17.4 17.3 17.1 16.8
7	to Fuze		7 / 5 / 4	1.10 Wil							` ,		
(2)		Faze .	P	(FS)									
C1		Table	Elwatin	(4 k)	E	311.5 31.56 319.7 323.9 328.1	3366 3452 3452	3540 358.5 363.0 367.5 372.1	376 8 381 4 386 1 390 9	400.5 405.4 410.4 415.4 420.4	425.5 430.7 435.9 441.1	451 8 457.2 462.7 468.3 473.9	479 6 485.3 491.1 497.0 503.0
		Range	D	(۲)	×	16200 16300 16400 16500	16500 16700 16800 16900 17000	17100 17200 17300 17400 17500	17600 17700 17800 17800 18000	18300 18300 18400 18500	18600 18800 18900 19000	19100 19300 19400 19500	19600 19700 19800 19900 20000

44699 60.143

97.2 97.7 98.9 98.9

.98 8 .99 4 .100 4 -101 0

468 150 158 458 458

0.000 0.000 0.000

-16 5 -16.7 -16 9 -17 1 -17.4

165 167 169 171

\$8888 4082 6-10

.959 .959 .179 .779 .883

-11 5 -10 9 -10 6 -10 3

-155 -157 -159 -161

155 157 161 163

-1043 -1058 -1059 -1059

848.00 84.00 94.00 94.00

-18.7 -18 9 -19 1 -19 4

18.6 19.1 19.3

88444

100.5 101.1 101.6 102.1

101.5 102.0 102.6 -103.2

34445 35445 369

-176 -178 -180 -182

175 177 180 182

4444

105 8 106.3 107.3

-107 0 -107 5 -108 0 -108 6 -109 1

88888

Table F(i)
CHARGE 9-SHELL 77B
Basic Data

		=	D JE JE	ا رم	Increase (+)	Z	ን _ት	799	77	°°°7	22555	44844	\$ 55 55 55 \$ 55 55 55	8 दे दे दे दे दे दे दे दे दे दे दे दे दे	æ¦r æ¦r	इङ्ह	3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
		- 01	Projectale Weight	(10 m _{pl})	Decrease Increase (+)	X	\$ 7 ;	114	2 5	5323	33333	3774°8	\$\$888	ಜಜಜಜಜ		5553	62 62 62 62 63
	$\Delta_{c} X$	6	% listac or D:ag		Increase (+)	Σ	107 8	888	1103	121	1125 11329 11336 1140	1145 115.0 115.5 116.1	117.5 118.3 119.1 119.5 119.5	119.7 120.8 122.6 125.0 125.0	1318	141.7	144 1 144 7 145 2 145 6 145 3
		∞	1% Ballistic Density of Drag Coefficient	(1%	Decrease (-)	X	-109.6	-1107-	-112.2	-1131	-1146 -1150 -1154 -1159	-116.7 -117.2 -117.5 -117.9	-1183 -1189 -1196 -1197	-120 2 -121 3 -123 2 -125 8 -129 1	-133	-1424 -143.5 -144.5 145.1	-1461 -1467 -1473 -1477 -1481
(ii)	Corrections to range for non-standard conditions Almude Sea Level	7	% oc Asr crature	T _B)	ncrease (+)	Σ	-1.1	-2.1 -2.6 -3.1	-36	44.0.0 9000		6.6.4.5.5 7.3.9.5.1	-110 -112 -114 -117	-126 -125 -122 -115	.93	1.28	+ + 1 1 1 2 4 + 1 2 4 4 5 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
e F	ge for non-standard Almude Sea Level	19	1 Saller	(1% T _B	Decrease [-)	X	-23 -18		77	13 7	2 2 4 4 4 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		, 103 109 11.5 12.4 13.6	14 4 14 14 14 14 14 0 12 9	114	w C1 % %	1.28 1.28 1.28 1.28 1.28
Table F(ii)	ge for no Almude	1	l Krox Ballusac Wind	183)	Tall (12)	X	-21 0	살살험	<u>:</u>	រ្យ់ឡង់រង <u>់</u>	<u> </u>	·	25.55.55.55.55.55.55.55.55.55.55.55.55.5	ដង់ដូងសូ ខ. » ព. ១ ១	. 30 S	215.25	31.7 31.7 31.7 31.7 31.7
C A	ns to rang	4		(1 KT 183)	REAL PROPERTY.	Z	210	21 S 21 7 22 0	22.2	2228 228 3028	**	22222 1422 4	26 7 27 1 27 8 23 8	28 5 29 3 29 3 30 2		2 2 2 2 3 1 3 1 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	31.9
	опестіо	3	SZIC CITY	. (%)	Increase (+)	Σ	-28 0	.283 284 285	-28 6	-287 -288 -289 -290	2925 2925 293 293 295	85 88 88 88 88 88	30.1 30.1 30.3 30.3	-30.4 -30.7 -31.0 -31.5	-328	35.2	.362 .362 .363 .363 .365
	O	1.10	1 M/S Muzzle Velocity	(11/5 1/9)	Decrease (.)	×	28 0	282 284 4	28 5	28 27 28 4 28 8 7 28 4 28 8 8 7 28 8	29 1 29 0 29 2 29 2 29 2 29 2 29 2 29 2	85538 42659	307 307 307 307 307	30.5 30.7 31.1 32.1	32.8	HARE HARE	35.8 35.8 36.0 36.0
		-	-	Range	();		20100 20200	2030 20105 30500	20600	20705 50805 50805 21000	21200 21200 21300 21300 21300	12 1500 12 17 17 17 17 17 17 17 17 17 17 17 17 17	22188 22188 22488 22488 22488	22700 22700 22700 22700	טטוצי	1308	87.55 88 88 88 88 86 88 86 86 86 86 86 86 86
				<u> </u>												}	turn Graff Build Street Street Street
	1		c 1		=	1	!									i	

	10	Correction to Corrector to change Height of Burst by Down 10M	points							 -			•
	6	Correction to Bearing for I knot cross wind	(1 KTH 2)	;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;	4 4 4 5 5 5 V	57. 57. 77. 78.	27. 27. 28. 80. 80.	. 3322	2 % % % % % % % % % % % % % % % % % % %	= = = -	885		
•	8	Correction to Beaning for drift	(de 1/2)	17.2 17.4 17.6 17.8 18.0	18.2 18.7 13.9 19.1	19.4 19.6 19.9 20.1	20.7 20.9 21.3 21.6 21.6	22.2 22.2 23.5 25.5	25.7 25.7 27.6 27.6 27.6	다. 당고 니_		41.0 42.1 43.1 44.0 45.0	
	7	Time of flight	(3)	55.5 56.0 56.6 57.1 57.6	58.2 58.8 59.3 60.5	61.7 61.7 62.4 63.0	64 4 65 1 65 8 66.5 67 3	68 0 68 9 70 6 71 5	72.6	-188 -1-88 -1-88	888 898 898 898 898	91.7	
Level	9	Fork	SE	44252	17 17 17 17	88866	នេះភេឌ	8 %%% 8	£%448	20 S	<u> </u>		
Basic Dala Altitude Sea Level	>	Effect on Range for increase of 1 mil in Firing Table	(AEFX/)	164 162 160 157 154	152 149 144 141	13.8	123	000 ever ex 8 - 1/4 4 4	77 73 8 6 1 7 7 8 8 7 7 7 8 8 7 7 7 8 8 7 7 7 8 8 7 7 7 8 8 7 7 8 8 7 8	: ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ;	1401	-8.5 -9.3 -10.4 -11.0	-
*	7	Correction to Fuze Setting to change Height of Burst by Down 10M	(PS /)		naganakan napa kir akir akir akir katalan sa								-
		Fuzc	(FS)			and the springers have been been a second and the second			, 	i			-
•	, ,	Firmg Table elevation	(4 _E)	\$09.1 \$15.2 \$21.5 \$27.8 \$34.2	\$40.8 \$47.4 \$54.2 \$61.0 \$68.0	575.2 582.5 589.9 597.6 605.4	613.4 621.6 630.1 638.7 647.8	6666 6666 676.8 687.5 688.7	724.1 724.1 738.6 754.8 774.9		927.9	954.9 862.2 976.1 985.5 985.5	_
		Rmgc	(x)	2500 2500 2500 2500 2500 2500 2500	2000 21000 21000	21100 21200 21300 21300 21500	22 22 20 20 20 20 20 20 20 20 20 20 20 2	2000 B	2352 2552 2552 2552 2552 2552 2552 2552	23.00	2000 2000 2000 2000 2000 2000 2000 200	222 222 222 222 222 222 222 222 222 22	
	ļ	1	1	1			67						

Table F(i)
CHARGE 9-SHELL 778
Basic Data
Attitude Sea Level

10	Correction	to "Corrector" 1 to change	, Haght of Burst by Down 10M		points								
6			or I knos cross wind	$\begin{pmatrix} \Delta_{C} & A_B \\ 1 \text{XTH}_{Z} \end{pmatrix}$	JE.	11.088	113	1.19	. 122	221 222 223 223 223 223 223 223 223 223	1.28	133	1338
04		Сотесноп	to Bearing for drift	(A. A.)	nlL	45.8 46.7 47.5~ 48.3 49.1	49.9 50.6 51.4 52.1 52.8	53.6 55.0 55.7 56.7	57.1 57.8 58.4 59.1 59.8	60.5 61.2 61.9 62.5 63.2	63.9 65.2 65.9 66.6	67.3 68.0 68.6 69.3 70.0	707 71.4 72.1 72.8 73.4
-		Į.	o, Iughi	Ξ	S	95.0 95.5 96.0 96.4	97.3 97.7 98.1 98.8	99.1 99.7 100.0 100.3	100.6 100.9 101.1 101.4	101.9 102.1 102.3 102.6 102.8	103 0 103 2 103.4 103 6 103.8	104.2 104.2 104.7	104.9 105.1 105.2 105.4
4	·		Fort	S	E	វា វ្នុជ្ធភ	7.1887.7	<u> </u>	44455	-127-13	11117	-100-100	22444
5	Effect on	Range for increase of 1 mil	in Firing Table	(Pryx/)	Σ	-126 -13.2 -140 -146	-15 8 -16.4 -16.9 -17 5	-18.5 -19.0 -19.6 -19.9 -20.2	-21.1 -21.4 -22.0 -22.5 -22.5	23.1 22.2 24.2 24.5 25.5	-25.8 -25.3 -26.3 -26.3	.27 7 .28 1 .28.1 .28.1 .23.4	-29.3 -29.5 -30.1 -30.3 -30.8
-	Correction	to Fuze Setting to	Height of Burst by Down 10M										
-	,		Fuze	(FS)									
-	-	i.	Teble	(46)	E	10022- 10100 1017.4 1024.4 1031.1	1037 6 1043.8 1049.9 1055.7	1056 8 1072.1 1077.3 - 1082.4 1087.3	1092.1 1096.8 1101.4 1105.9 1110.3	1114.6 1118 9 1123 0 1127.1 1131 2	1135 j 1139 0 1142,9 1146,6 1150,4	11540 1157.7 1161.2 1164.8	1171.7 1175.1 1178.4 1161.7 1185.0
-	-		Range	χ	Z	2220 22100 22000 21800	21730 21560 21580 21580 21400	21200 21100 211000 20900 20800	20700 20600 20500 20400 20300	20200 20100 20000 19900 19800	19700 19600 19500 19400 19300	19200 19100 19000 18900 18800	18700 18600 18500 18400 18300

Table F(ii)
CHARGE 9 - SHELL 778
Corrections to reget for non-standard conditions
Albrude Sea Level

=	Projectile Weight	(10 m _n ,)	Decrease Increase	X	 &&&&&	\$\$\$\$ \$, \$ & & & & & & & & & & & & & & & & & &	62 62 63 64 65	<u> </u>	60 -59 -59 -59 -59 -59	58 57 57 57	રું <u>રું</u> રું રું કર્
0	₽.≠	0.)	Decrease (·)	Σ	62 61 61 61	22288	88888	27.28.88.88	አጸጸጸጸ	SSKKK	22222	28888
0	19. Ballistic Density of Drag Coefficient	, D _B)	Increase (+)	Σ	145 9 146 0 146 0 145 9 145 9	1457 1456 1454 1452 1449	1446 1442 1438 1429	1428 1420 1415 1410	139.9 138.9 138.9 135.3	1373 1367 1362 1352 1352	1347 1336 1331 1325	131 9 131 3 130 7 130 1 129.5
8	Ba Densit	(1%	Decrease (-)	Σ	-1483 -1484 -1484 -1484 -1484	-1482 -1479 -1476 -1473	-146 6 146 2 -145 9 -145.5	-1446 -1442 -1436 -1431-	-1421 -141.6 -1411 -1407	-139 9 -139 4 -139 0 -137 9	-1373 -1367 -1362 -1356 -1351	-134 S -134 0 -132 9 -132 9
- 3	1 % Ballistic Aur Temperatur	eTs)	Occrease Increase	Σ	552738 552738	464 7.57 177 177	+777 +79 +82 +84 +86	4 4 6 4 4 6 4 4 6 4 6 4 6 4 6 4 6 4 6 4	+96 +97 +100 +10.1	+102 +103 +104 +105	+1107 +1109 +1110 +111.1	++1113
9	Belli. Temp	(187		ž	647.7.6	86 86 66 66 86 86 86 86 86	-10 1 -17 9 -10 6 -10 9 -11 1	-11.6	1227	137	-142 -144 -146	-14 8 -14 9 -15 1 -15 2
~	1 kms Palisco: Wen:	. H.	[五]	Σ		13.12 13.13	<u>ૡ૿ૡ૽ૡૢૹૢ</u> ઌઌઌઌ	<u> </u>	88888 84888	<u> </u>	ង់ង់ង់ង់ង់ 2.3.3.2.4	**************************************
7	-8=	(1 KT H'R	華	I	325.5	33.7	3333	33.00.03	88888 817.8881	38888	30 0 30 0 29.9 29.8	2888 347 347
3	1 M/S Muzzle Velocity	(o 1 s	Increase (+)	Σ	.365 .365 .360 .370	370 370 370 369	368 368 367 367	366 366 365 365 365	-363 -363 -361 -361 -361	360 359 358 358 357	.356 .355 .354 .354	.352 .35.1 .349 .349
2	- 52	(1M/s 1/0	Dormase (-)	X	3633 3633 3643 3643 3643 3643 3643 3643	36.4 36.4 36.4 36.4 36.4	363 362 362 361	35.9 35.9 35.9 35.8	35.5 35.5 35.3 35.3	XXXX3 78.501	***** 8	340 33.9 33.8 33.8 33.6
1	R	k !	(x)	Σ	22200 22100 22000 22000 21000 21800	21700 21600 21500 21400 21300	21200 21100 21000 20800 20800	20700 20600 20500 20400 20300	20200 20100 20100 20000 19800 19800	19700 19600 19500 19400 19300	19200 19100 19000 18900 18800	18700 18600 18500 18400 18300
ı	I			1 }			post hart some hagh stag in	the board about board again	t tring arms bent turn user	Vertil Street Street Street Street St	and allowed broad formal games	larine name auton busin busin

Table F(i)
CHARGE 9-SHELL 77B
Basic Data
Altitude Sea Level

					٠							
10	Correction to	to change Height of Burst by Down 10M		points								
6		Bearing for 1 knot cross wind	$\binom{\Delta_{C}}{1} \binom{A_B}{1} \binom{N}{2}$	JE:	1411143	146 147 148 149 150	25.52.52	1.57	29 29 29 29 29 29 29	1 69 1 70 1 71 1 73	1.75	1 83 1 84 1 85 1 87
00		Correction to Bearing for duft	(4x, 24)	μL	74 1 74 8 75 5 . 76 3	77.7 78.4 79.1 79.8 80.5	813 820 827 83.5	85.0 85.7 86.5 87.2 88 0	%%% %%% 91.1 91.0	92.7 93.5 94.3 95.1	97.7 97.8 98.1 180.0	100.8 101.7 102.5 103.3
1		Tume of Night	Ξ	S	1057 1059 1060 1063	201 108.6 107.0 107.0	107 1 107 2 107 4 107 5 107 6	107.7 107.9 108.0 108 1 108 2	108 3 108 4 108 5 108.6 108.7	108 8 108 9 109 0 109 1 109 1	200 200 200 200 200 200 200 200 200 200	8 601 109.9 100 0 110 0
2		Fork	S	16	ئ ۈۈۈۈ	∞ ∞ ∞ ∞ ∞	8 8 8 8 L L	<i></i>	ンレタカカ	φφφφφ	φ φνννν	ふふふふ か
20 20 1	Effect on Range for	of 1 mil of 1 mil in Firing Table	(CEFX/)	Σ	-31.0 -31.3 -31.8 -32.0 -32.0	33.3.3.3.3.3.4.3.4.3.4.4.4.4.4.4.4.4.4.	444 444 353 366 366	-36.6 -36.6 -36.9 -37.2 -38.3	2,82 2,82 2,90 8,90 8,90 8,90 8,90	8 4 4 4 4 8 4 4 4 4 4 4 4 4 4 4 4 4 4 4	44544	44124 00202
6	Correction to Fuze	change Change Height of Burst by	(Ac FS/)				•					
(*		Fuzc setting	(FS)									
6		Funng Table clevation	(A _E)	E	1188 2 1191 4 1194 6 1197 7 1200 8	1203 8 1206 8 1209 8 12128 12128	1218 6 1221 5 1224 4 1227.2 1230 0	1232.7 1235.5 1738.2 1240.9	12.16.2 12.18.4 12.51.4 12.53.9	1259.0 1261.5 1264.0 1266.4 1268.8	1271 2 1273 6 1276 0 1278 3 1280 7	1283 0 1285 2 1287 5 1289.7 1289.7
-		Range	(x)	×	1 AT AM THE BUT A	17700 17700 17700 17700 17700	1720 17100 17000 16900 16900	26 50 50 50 50 50 50 50 50 50 50 50 50 50	15 15 15 15 15 15 15 15 15 15 15 15 15 1	15.00 15.00 15.00 15.00 15.00 15.00	25.25.35.35.35.35.35.35.35.35.35.35.35.35.35	14500 14500 14500 14500

Table F(ii) CHARGE 9-SHELL 77B

Corrections to range for non-standard conditions $\Delta_{C} X$ Altitude Sea Level

=	11	1□ Projectile Weight	(1□ m _{py})	Increase (+)	×	~~~ ? ? ? ? ? ? ? ? ? ?	<u>፟</u> ጵጵጵጵጵ	\$\displays{2} \displays{2} \dis	54444 888	88888 88888	7777	7747=	339999
9	6 10	Proj	(10	Decrease	Σ	48 48 48 47	44444 6444	2444	44666	, 447 472 473 473 473 473 473 473 473 473 473 473	40 40 30 30 30	338	37 38 35 35 35
		1% Ballistic Density or Drag	$(1\% D_B)$	Increase (+)	X	128 8 128.2 127.6 127.0	1257 1251 1245 1238 1238	1226 1220 1213 1213 1207	1194 1188 1181 1175	1162 115.5 114.8 114.1 113.4	1125 1117 1109 1100	108 4 107 6 106 7 105 9 105 9	1042 1034 1025 1016 1016
		Ball Density	. 1%	Decrease (-)	×	-131 8 -131 3 -130 8 -130 2	82778	-1256 -1248 -1241 -1234	-121 9 -121.2 -120 4 -119 6 -118 7	-1178 -1169 -1161 -1152 -1144	-113.7 -112.9 -112.2 -111.4	109 8 -109 0 -108 2 -107 4	-105.7 -104 8 -103 9 -103 0
	7	1 % Ballıstic Aır Temperature	T _B)	Increase (+)	X	+116	+120 +120 +121 +121	+1223 +1233 +1233 +1233	+124 +124 +124 +124 +125	+12.5 +12.5 +12.5 +12.5 +12.5	+125 +125 +124 +124 +124	+1553 +1523 +1523 +1523	+121 +121 +120 +120 +119
Allilude Sea Level	9	Ballist Tempo	(18	Doctease (-)	M	-154 -154 -155	NUNUN	-15.7 -15.7 -15.7 -15.7	-157 -157 -157 -157	.15 6 .15 5 .15 4 .15 4	-153 -153 -152 -152 -151	-150 -149 -148	-146 -145 -145 -143
Aumud	3 4	1 Knot Ballistic Wind	W_B)	[13] (34)	M	-28 9 -28 8 -28 7 -28 7		-28 0 -27 9 -27 8 -27.1 -27.1	-27 4 -27 3 -27 2 -27 1 -27 0	-269 -267 -265 -265	-82 -261 -260 -258 -258	255 253 250 250 218	24.7 24.5 24.3 24.1 23.9
		1 F Bal	(1 KT 1 8/8)	H899	X	293 292 291 290 280	28 2 2 2 2 2 2 3 2 3 4 4 4 4 4 4 4 4 4 4 4	28.3 28.3 28.2 28.1 28.0	279 278 27.7 27.6 27.5	27.4 27.3 27.2 27.1 27.0	88888 8578 845	283 280 250 250	2222 24 20 20 20
		1 NVS Muzzle Velocity	1 % S	Increase (+)	M	.24. .24. .24.	3339	.334 -333 -33.1 -32.8	-327 -328 -324 -322 -321	319 317 314 318	.31 0 .30 9 .30 7 .30 5	.302 -300 -298 -298 -294	-23 2 -29 0 -28 8 -28 6 -28 6
	C1	Velo	(1 m/s 1/2)	Decrease (-)	Σ	33.4	1 44444	322 321 319 318 316	31.5	30.8 30.5 30.5 30.2	301 299 297 296 296	292 289 287 287	28.2 28.2 28.0 27.9
	_		Range	(X)	M	18200 18100 18000 17900	17788 17680 17580 17480 17380	17200 17100 17000 16900 16800	16700 16600 16500 16400 16300	16200 16100 16000 15900 15800	15700 15600 15500 15300 15300	15200 15100 15000 14000	14700 14800 14400 14400
			LE.	•				ne door stand stand stand based			, mas and ton past tool		

Table F(i)

CHARGE 9 - SHELL 77B Basic Data Attitude Sea Level

		R			·
	10	Correction to the control of the c	points		
	6	Correction to Bearing for 1 knot cross wind (\(\Delta_C A_B \)/(1)\text{FT}\)	¥	27 27	•
	00	Correction to Bearing for drift (\(\Lambda_{\mathcal{A}} A_{\mathcal{A}} \))	ηL	0 20 5 0 1 0 2 8 8 8	
	-	Tume of flight	S	110.3	
rever	9	Fork	E	సస	•
Auruae sea Leve	5	Effect on Range for increase of 1 mul in Finng Table clevation (\(\frac{\rho_{E,F}X}{\rho_{E,F}X} \)	Σ	4 4 6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	
1	7	Correction Effect on to Fuze Sering to Increase change of 1 miles Bursh by I Table Down 16M elevation (Ac FS I)			
	5	Fuze scining (FS)			
	۲،	Finng Table cievation (A.F.)	E	123% 3	
	-	Rupe (X)	Z	14100	

Table F(ii) CHARGE 9.SHELL 77B

Corrections to reger for non-standard conditions $-\Delta_{\mathcal{C}}\,\lambda$

Alunde Sea Level

10 , 11	LD Sycology	W cigh	(10 E.y. /	ascilic	-	33 -36	 	ma ^{mo} = especia				lementale di cita em			
6 3	19. Rallicic	Density or Drag Coefficient	(1% D _B)	Docreuse Increase D		988			A						
8 1 6 1	1 %		$(1\%T_B)$ (Decrease Increase Decr	X X	+118 +118 -1001 +117 -992									
9					M M	.337 -142 -334 -141 -332 -139	 	 		···				*	
77	1 K53 - 9	13.13	(1 KT W.)	(H) (H)	N	24 8 24 5 24 5 24 5 24 5 24 5 24 5 24 5									
	1 M/S	Velocin	(1M/s V.)	Decrease Increase	M								`		
2		ξ >	× -	Decress (-)	Σ	27.5 27.3 27.1	 								
-		ć	Kange	(x)	Z	1 14200 1 14100 1 14000									
10	10 10 10 10 10 10 10 10 1	10 change Heicht of	Burst by		, points		 	 Now tonigne date				 			

Explanatory Notes on 155mm BOFORS Range Tables (RT)

Basic Data (Table F (i)) Column No. Description Range (X): Range in m, being aimed 1 Firing Table Elevation (A_E). Elevation in mils (360 deg = 6400 mils) to be set on the gun to achieve range at col. 1. 3 Fuze setting (FS) setting to be done on the fuze so that it functions(bursts during flight) at the time mentioned at col. 4 (in case time fuze being used) 4 Corrn to fuze setting(FS) to change height of burst by down 10 m. 5 Effect on range, in m, for increase of 1 mil in firing table elevation 6 Fork (also known as short bracket): when a large no of shells are fired at the MV and elevation in a series (i.e. in quick succession) they will exhibit some dispersion pattern, which (supposedly) follows normal statistical distribution. The x(range) and y (cross range) co-ordinates of fall of shot are treated separately as independent variables and the standard deviation $\sigma_x \& \sigma_y$ in x & y resp. are obtained 50 % zone in range and cross range is defined as the length zone spread equally around the mean point of impact (more commonly known as MPI) of a series of rounds fired which may contain 50% of the rounds if a large no. of rounds are fired. 50% Zone = 1.349 σ_x (or σ_v as applicable) Half the 50% zone is known as probable error, i.e 50% zone consists of one probable error on either side of the MPI. Fork: the change in elevation required to produce a range change equivalent to 4 x range probable errors. This parameter is mainly used for range safety purposes. 7 Time of flight: the time taken by the projectile to travel from the moments it leaves the gun barrel to the point of impact. 8 Correction to Bearing for drift. The angular correction to be applied to the line of fire called bearing (bearing is the angle measured clockwise from local North) to compensate for the deviation of the shell from the line of fire towards right due to its right hand spin. Most of the artillery shell are gyro. stabilized hence have an eq-m total angle of attack (called yaw of repose in ballistics) towards right and upwards wrt the velocity vector resulting in the deviation of projectile to right of line of fire. 9 Correction to bearing for 1 knot cross wind: corrn to be provided to the bearing of line of fire to nullify the deviation of the shell due to constant cross wind of 1 Knot magnitude through out the trajectory at all heights. The correction is - ve if the crosswind is blowing from Lt to Rt i.e. + vel cross wind. In practice the wind will never be constant, at all heights. A weighted mean value (wrt heights) is obtained called as equivalent constant wind (ECW) A wind of quantity ECW will produce the same effect as that of the actual-prevailing wind. Hence for the same prevailing wind conditions ECW values will be different for different ranges due to the difference in the vertex heights. Same thing is applicable in case of range i.e. head or tail wind. The measured wind data at different is first resolved in to range and cross wind components at all heights. Equivalent constant winds for range and cross components are calculated and used separately. Corrn to "corrector" to change height of burst by down 10 m. 10

Correction to range for non-standard conditions (Table F (ii));

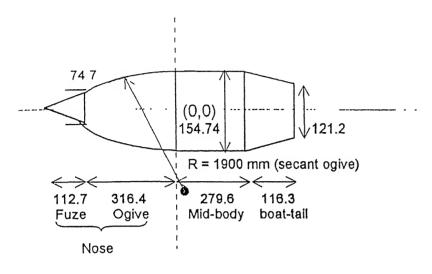
Column No.	Description
2 & 3	Rango (X): Rango in m, boing aimed Correction to range in m for a change in muzzle velocity (MV) by 1 m/s If the MV increases then the range also increases, hence the correction to range for increase in MV is -ve
4 & 5	Correction to range in m for a range wind of magnitude 1 knot A tail wind is taken as +ve & head wind –ve If it is tail wind then the range increases, hence the correction to range is -ve
6 & 7	Correction to range in m for a change in ballistic air temp—by 1% of the standard. The RT is compiled for some standard meteorological conditions, which defines the air temp, pressure and density at various altitudes. In case of 155mm RT ICAO standard atmosphere is assumed Air is assumed to be dry in ICAO but in practice it may have some moisture. Also the temp and press may not be the same as the standard Ballistic air temp. (BAT): BAT is the temp. of the dry air having an equal density as that of moist air. The correction for BAT only takes care of the changes in range on account of the changes in Mach No. due to variation in temp. (recall that acuastic velocity = $\sqrt{(\Upsilon RT)}$) and not the variation in density due to changes in temp. This is also termed as elasticity effects.
8 & 9	Correction to range in m for a change in ballistic density (ρ) or change in drag coefficient (C_D)by 1 %. If ρ or C_D increases then the range decreases, hence the correction to range is +ve. Density at different altitudes will be different, however a single weighted mean value is obtained (in the same manner in which wind is treated).
10 & 11	Projectile weight: Correction to range for a projectile whose weight differs from the standard weight by 1 unit (\square m _{pl} : \square marking is done on the shells after manufacture for there identification in terms of weight class. One such square means that the shell weight differs from the std. by 1 unit). The method of marking is different for different equipments, The effect of change in shell weight is two fold: first the MV reduces resulting in the reduction in range and second the carrying capacity increases (Drag / Mass decreases i.e. less deceleration than the normal) resulting in increase in range. The net effect could be either way. For shell HE 77B 1(\square m _{pl})= 0.450 kg

Explanation about "Ammunition Data(cont.)" on page (x)

Shell weight influence:-

The relationship given there viz. Δ Mv = A2 x Δ 100 g shell weight,

Gives the change(decrease) in muzzle velocity (Mv) due to 100 gm change(increase) in the shell weight for various charges (M3A1 3G etc are designated propellant charges with fixed qty of propellant. Each charge corresponds to a certain Mv. It can be seen that the shell influence is increasing as the Mv increases (from top to bottom)



Total Length = 825 mm

CG Location = 533 mm from Nose-tip

Moment of Inertia

Axial, $I_{XX} = 0.146 \text{ kg-m}^2$

Transverse, $I_{YY} = 1.709 \text{ kg-m}^2$ (through an axis passing through CG)

Twist of Rifling(n) = 1 in 20 calibres. \Rightarrow the shell will complete

one full rotation (360°), in side the gun barrel by the time it does a translation or linear travel of 20

calibres i.e. 20 * 0.155 = 3.1 m.

Thus launch spin = Mv / (n.d) = 818 / (20 * 0.155) = 263.87 rev/s = 15832 rpm

Fig A1. Schematic of 155 mm Bofors Shell HE 77B

Appendix B

FEED FORWARD NEURAL NETWORK

The back propagation network consists of one input layer, one output layer and one or more hidden layers. There is no theoretical limit on the number of hidden layers but typically there is just one or two. Some work has been done [14], which indicates that minimums of four layers (three hidden layers and one output layer) are required to solve problems of any complexities. Each layer is fully connected to the succeeding layer (standard connection).

There are as many neurons in the input layer as there are inputs, and likewise with the output layer. The number of layers and the number of neurons in the hidden layer(s) must be determined by trial and error. There is no quantifiable best answer to the layout of the network for any particular application. There are only general rules picked up over time and followed by most researchers and engineers applying various architectures to their problems.

- Rule 1. As the complexities in the relationship between the input data and the desired output increases, the number of processing elements in the hidden layer should increase.
- Rule 2. If the process being modeled is separable into multiple stages, then additional hidden layers may be required. If the process is not separable into stages, then additional layers may simply enable memorization and not a true general solution.
- Rule 3. The amount of available training data sets an upper bound for the number of processing elements in the hidden layer. To calculate this upper bound, use the number of input-output pair examples in the training set and divide that number by the total number of input and output processing elements in the network. Then divide the result again by a scaling factor between five and ten. Larger scaling factors are used for noisy data.

Extremely noisy data may require a factor of twenty or even fifty. Very clean input data with an exact relationship to the output might allow the factor to be dropped to around two.

Cross-Validation and Overtraining

One approach to avoid over-training of the network is to estimate the generalization ability during training and stop when it begins to decrease. The essence of back-propagation learning is to encode an input-output relation, presented by a set of data, with a multiplayer perceptron well trained in the sense that it learns enough about the past to generalize to the future. The simplest method is to randomly partition the data set into a training set and a test (validation) set. From the training set, a validation subset, which are typically 10 to 20 percent of the training set is set aside. The motivation here to validate the model on a data set different from the training set that is used for selecting the architecture of the network. The training set is used to modify the weights, the validation set is used to estimate the generalization ability. The architecture of the network is varied till the training set results in MSE less than the prescribed value ε . This architecture is now tested on the test data (which can be one or more) and if the MSE is of the order of 2ε , the architecture is accepted to yield the desired neural model and assumed to be capable of predicting required output for inputs not seen earlier by the network.

Another way of avoiding over-training is to limit the ability of the network to take advantage of spurious correlation in the data. Over fitting is thought to happen when the network has more degrees-of-freedom (the number of weights, roughly) than the number of the training samples when there are not enough examples to constrain the network.

Even though it may give exactly right output at the training points, it may be very inaccurate at other points. An example is a higher order polynomial fitted through a small number of points.

Sufficient Training Set Size For a Valid Generalization

Generalization is influenced by three factors: i) the size and the efficiency of the training set, ii) the architecture of the network, and iii) the physical complexities of the problem at hand. Clearly, we have no control over the last factor, i.e., the physical complexity. We have already discussed the choice of architecture based on training and test data. Once the architecture of the network is fixed, then the size of training set can be derived as follows.

Let M denote the total number of hidden layer computation nodes. Let W and N be the total number of synaptic weights and the number of random examples used to train the network respectively. Let ϵ denote the fraction of error permitted on test. Then, according to Baum and Haussler, [2] the network will almost certainly provide generalization provided the following two conditions are met.

- (a) The fraction of error made on the training set is less than $\varepsilon/2$.
- (b) The number of examples(N) used in the training is

$$N \ge 32 \frac{W}{\varepsilon} \ln \frac{W}{\varepsilon}$$

where W is the total number of synaptic weights.

Ignoring the logarithmic factor, taking first order approximation, the number of training examples is directly proportional to the number of weights in the network and inversely

proportional to the accuracy parameter ϵ . Then, $N > \frac{W}{\epsilon}$.